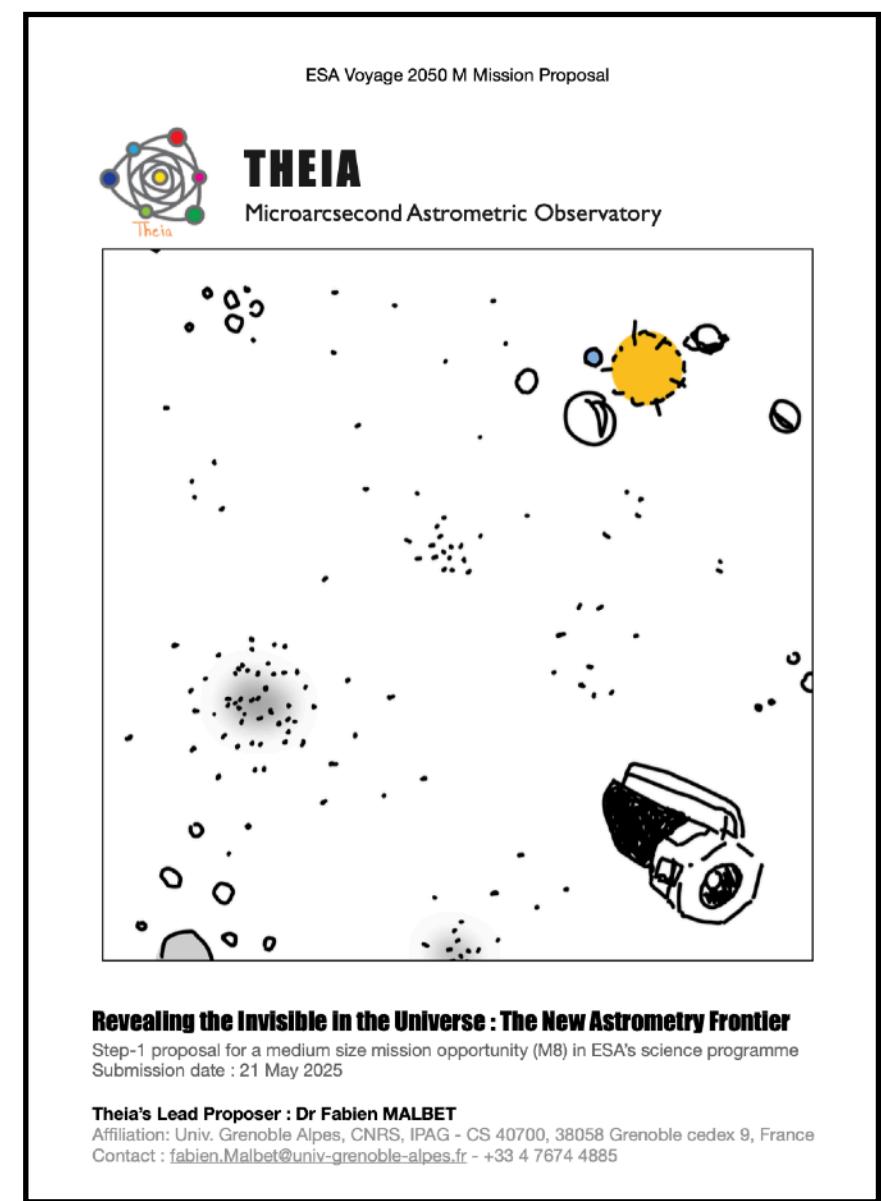


Metrology studies for high precision astrometry in Theia / HWO

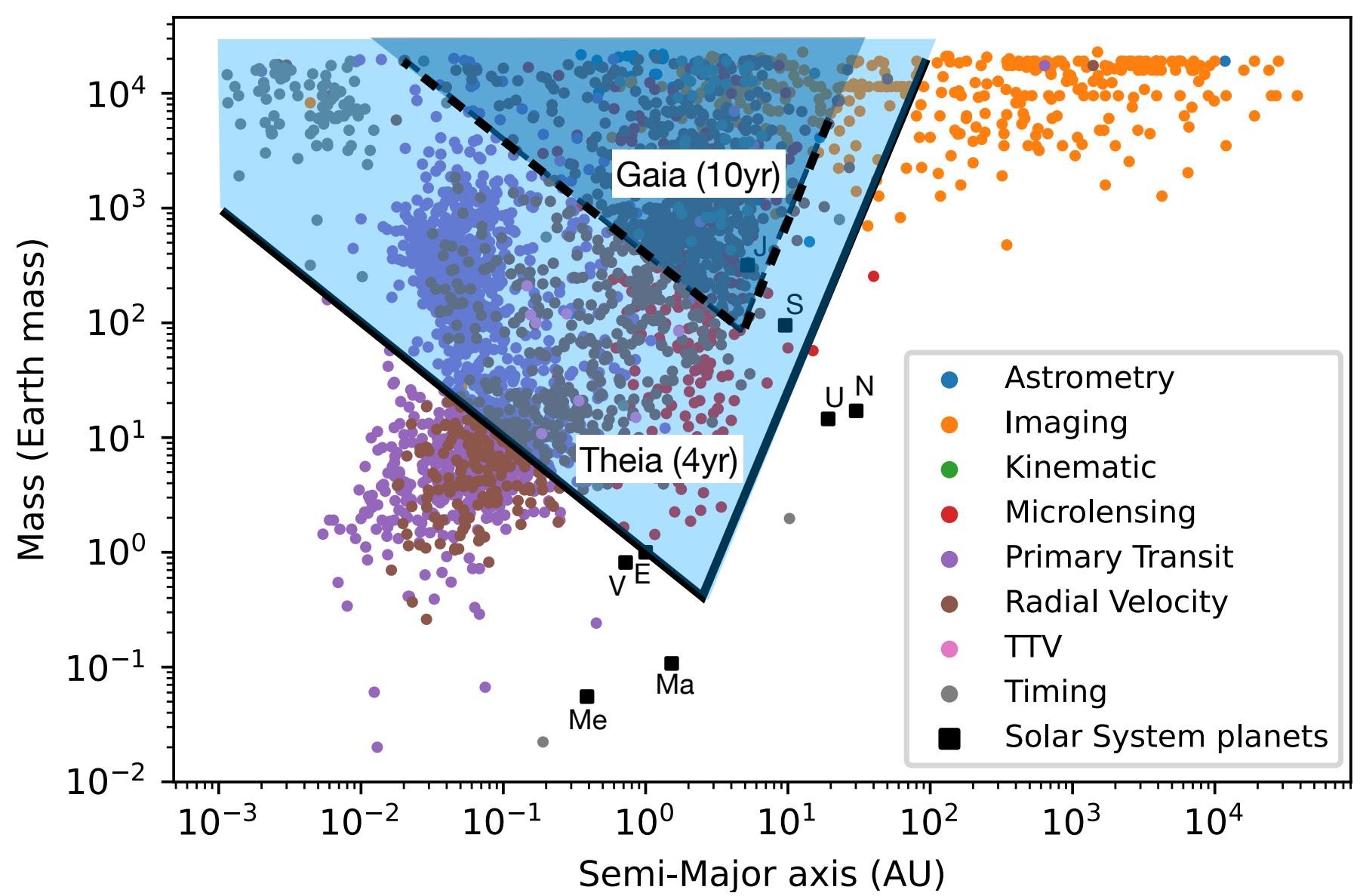


Fabien MALBET
IPAG / Univ. Grenoble Alpes / CNRS

*with M. Lizzana, F. Pancher, S. Soler, H. Rousset, Y. Er-Rahmaouy, Y. Bakka @IPAG
and A. Léger, (IAS) T. Lépine (IOGS/University. St-Etienne), A. Sozzetti (INAF Torino), L. Labadie (University. Köln)*



Theia proposal for ESA M8



Context of the studies

- **High precision space astrometry in the visible domain**
 - Earth-mass planets orbiting in the Habitable Zone of nearby solar-type stars
=> Bright star mode with requirement
 - Investigating the nature of Dark Matter through the shape of dwarf spheroidal galaxies (cored or cuspy ?), the kinematic disturbances for stars above/below Galactic plane, and the direction of proper motion for hypervelocity stars

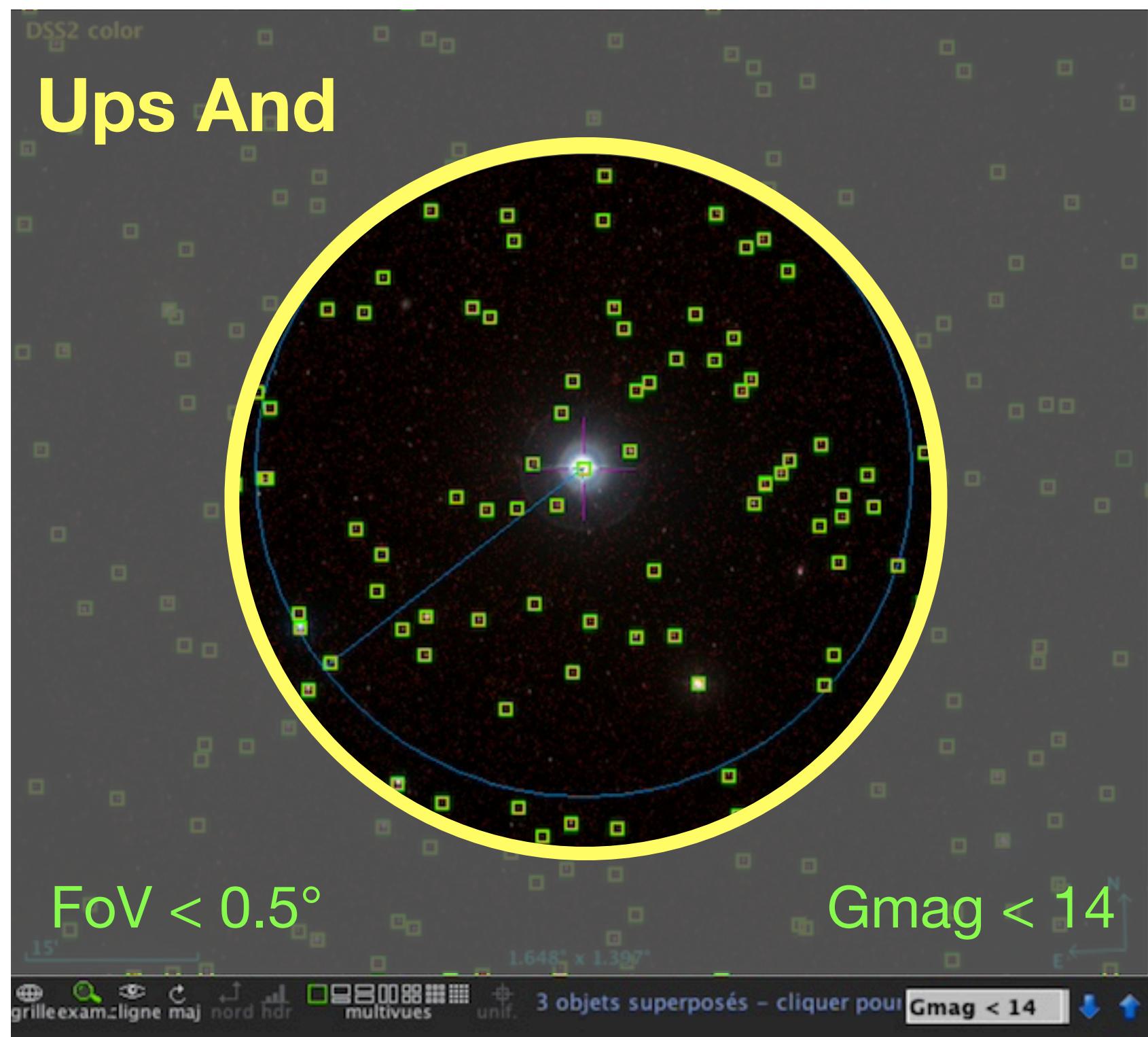
- **Two application projects**

- **Theia**: 0.8-m telescope with FoV of 0.7 degrees (ESA M8)
- **HWO** 7-m telescope high resolution imager with 3'x2' FoV (NASA)

- **Differential pointed astrometry**

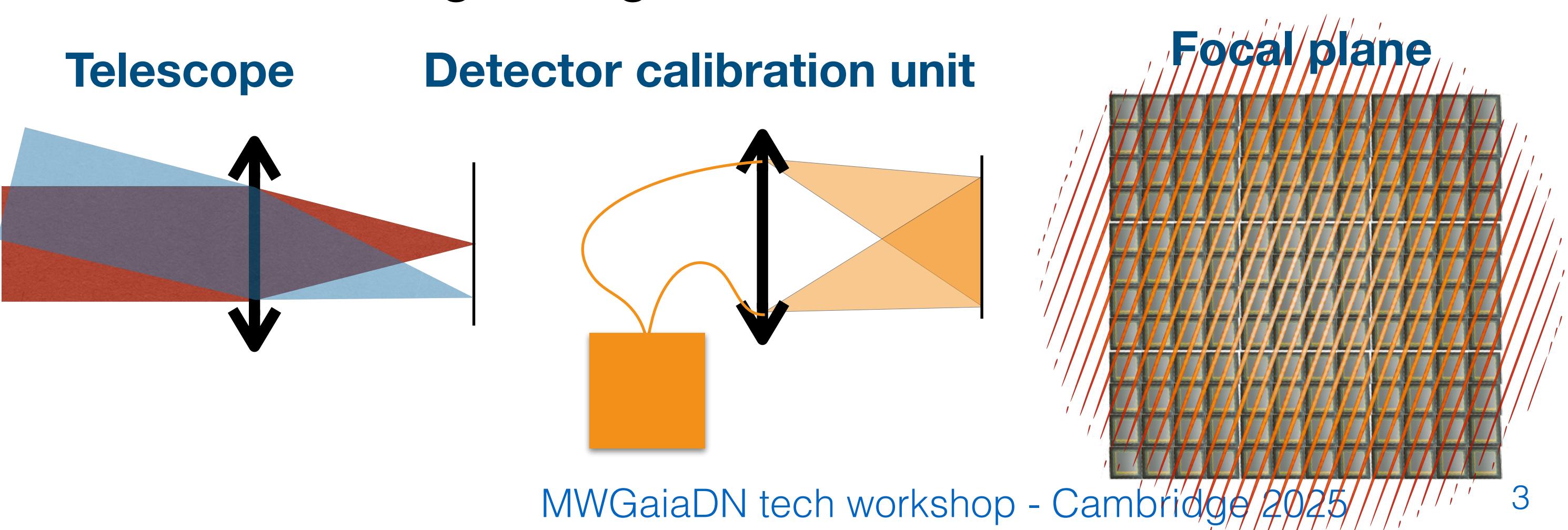
- Gaia global astrometry allows data closure over the sky but is limited in exposure time and number of visits
- Pointed astrometry allows optimization of exposure time and observing sequences, but fewer objects

Principle : relative and precise differential astrometry

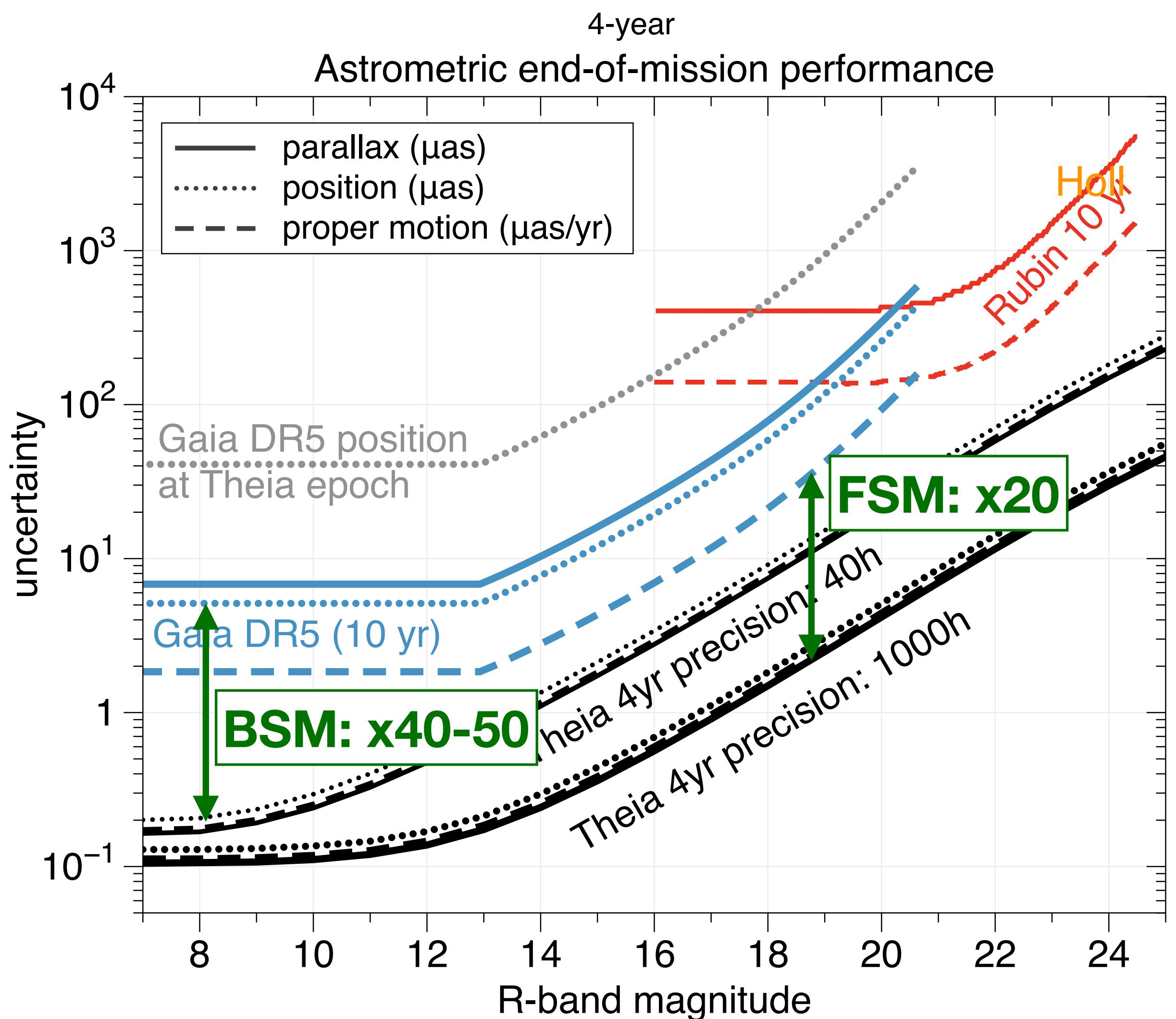


Gaia DR3 data

- ✓ The science target is at the center of the FOV
- ✓ We measure the offset angles between the target object (in the center) and the reference stars (other stars in green)
- ✓ The single measurement is repeated several times over the mission lifetime to reach the required accuracy on the target motion
- ✓ The detector calibration is done using interferometric modulated Young's fringes



Theia expected performances



- **Faint Source Mode (FSM)** : 23 times the PM precision of Gaia (10yr) and 14 times that of HST (10yr)
- **Bright Source Mode (BSM)** Theia's 1 μas precision in 1h integrations at the reference value $R = 10\text{mag}$ exceeds that of Gaia by factor of ~40-50, Roman ~10-20 and VLTI/GRAVITY by ~30-100, and other missions/instruments (e.g. HST, JWST, ELT/MICADO, Rubin) by even larger factors.

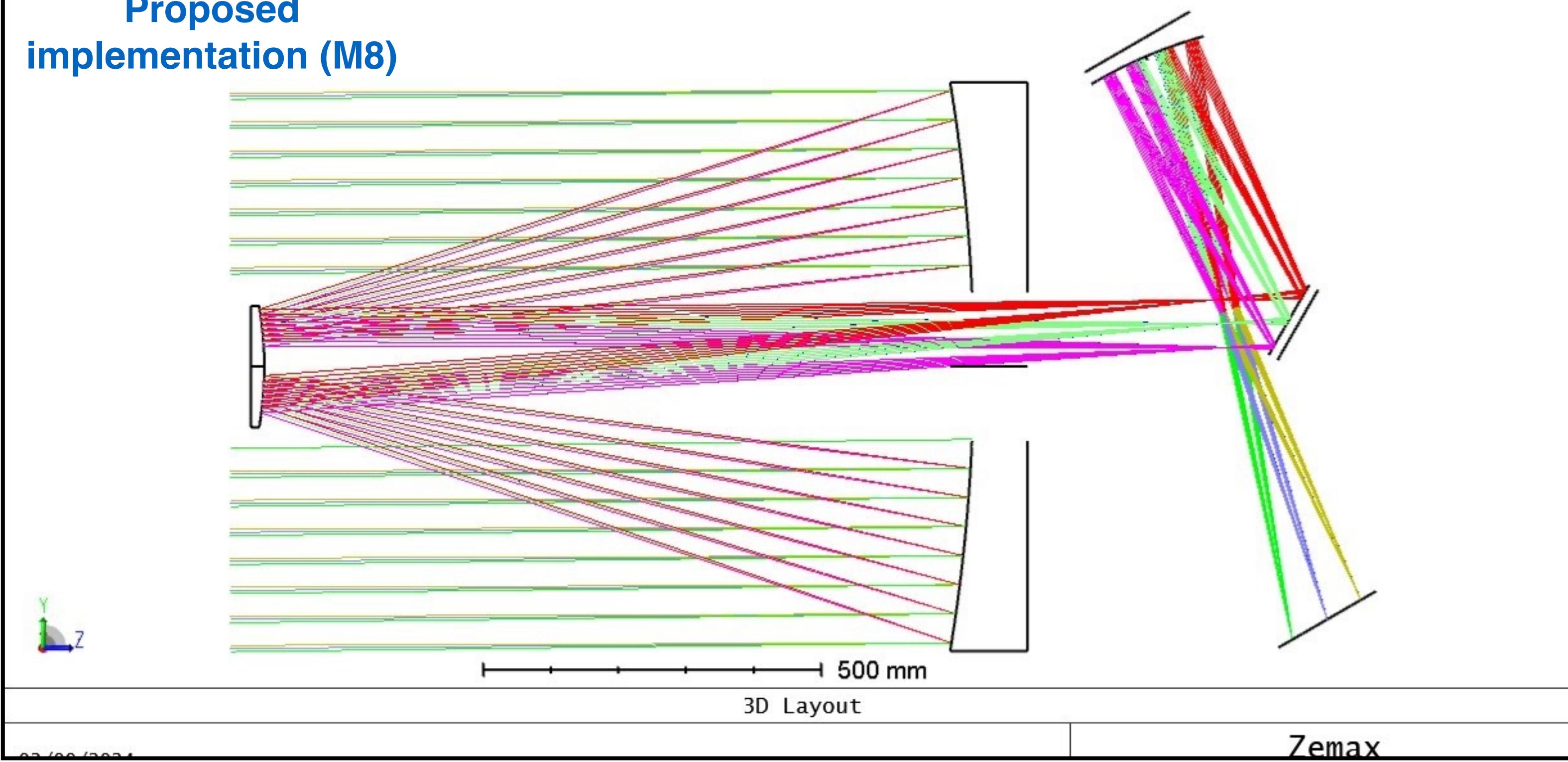
Theia optical concept (ESA M8)

Spot Diagram

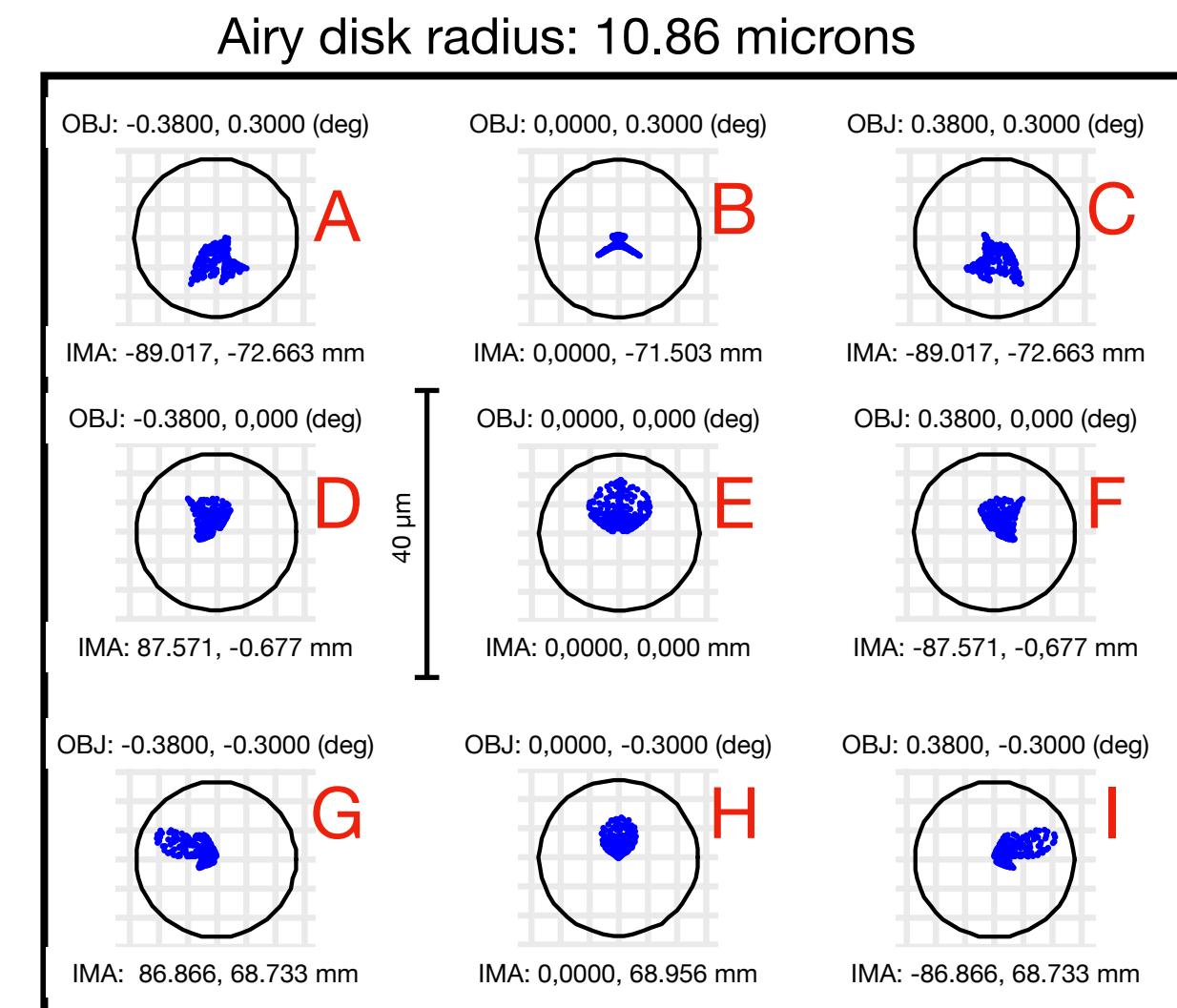
Theia characteristics :

- 0.8-m telescope diameter
- diffraction-limited 0.5° FOV

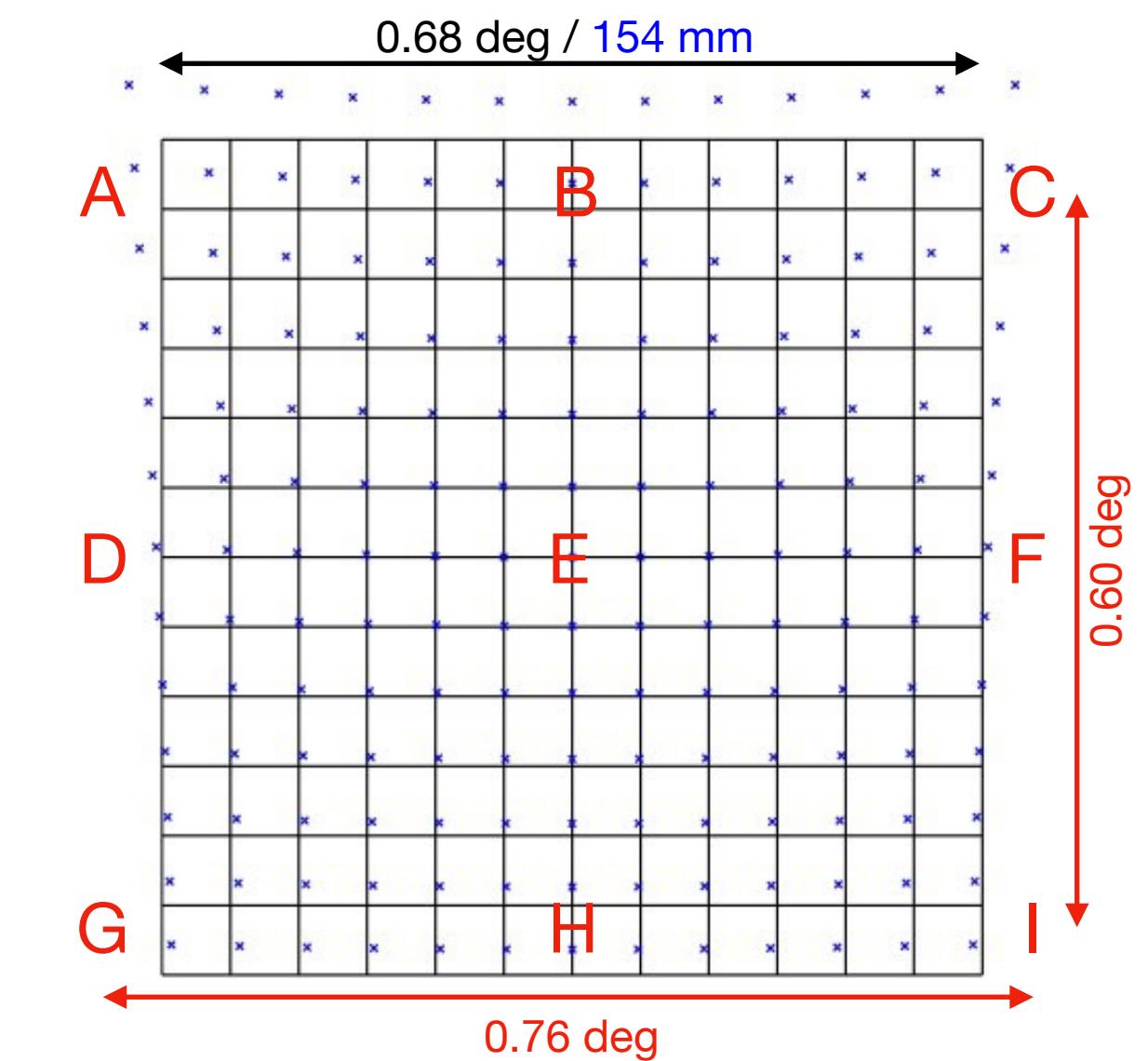
Proposed implementation (M8)



Three mirror anastigmat, Korsch design



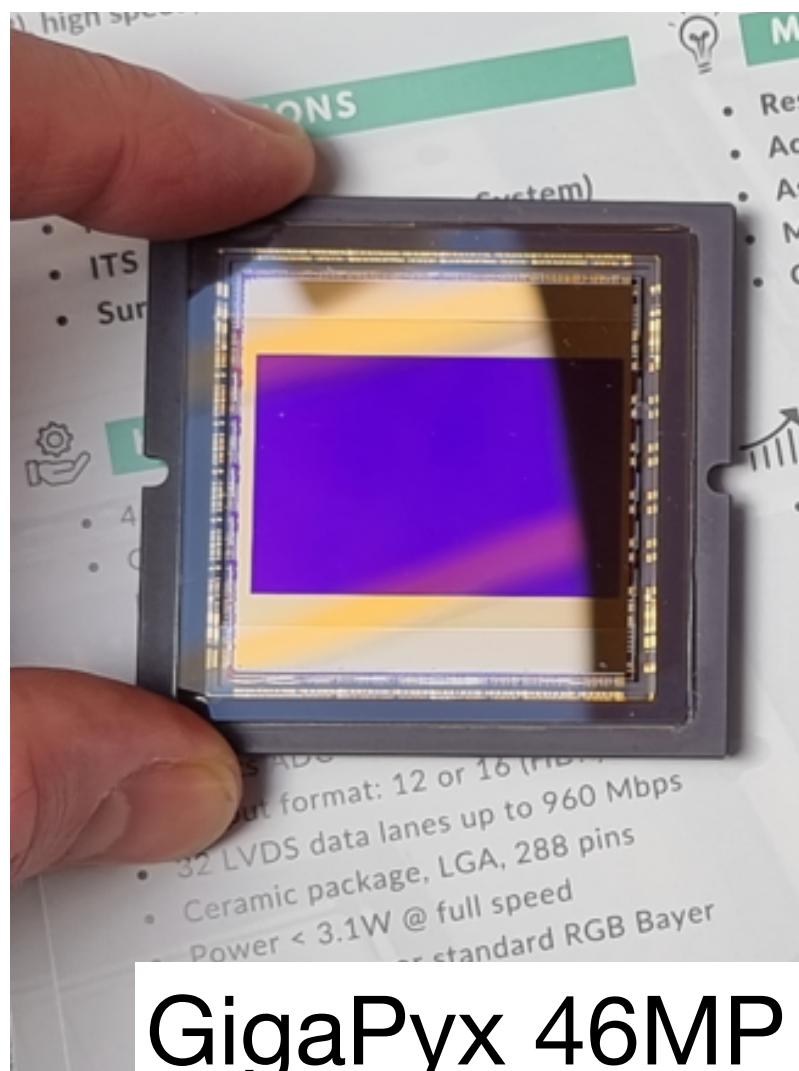
Distortion map 13x13



Focal plane for Theia

The Focal Plane uses 4 Pyxalis CMOS detectors
GIGA220M (in development) +1 GIGA14M:

- 4x [16640 x 13156 pixels] (4 x 218 915 840 pixels) + 1 x [4160 x 3256 pixels] with 4,4 um pixel pitch
- Non buttable (~10 mm on 2 sides / ~2 mm on 2 sides): 27% loss of area
- Focal Plane 173 mm x 136 mm
 $\Leftrightarrow 45.7 \text{ arcmin} \times 35.9 \text{ arcmin}$
 $\Leftrightarrow 0.76^\circ \times 0.60^\circ$
- **0.46 deg² total for 0.33 deg²**
effective (881 Mpx), i.e. 27% loss



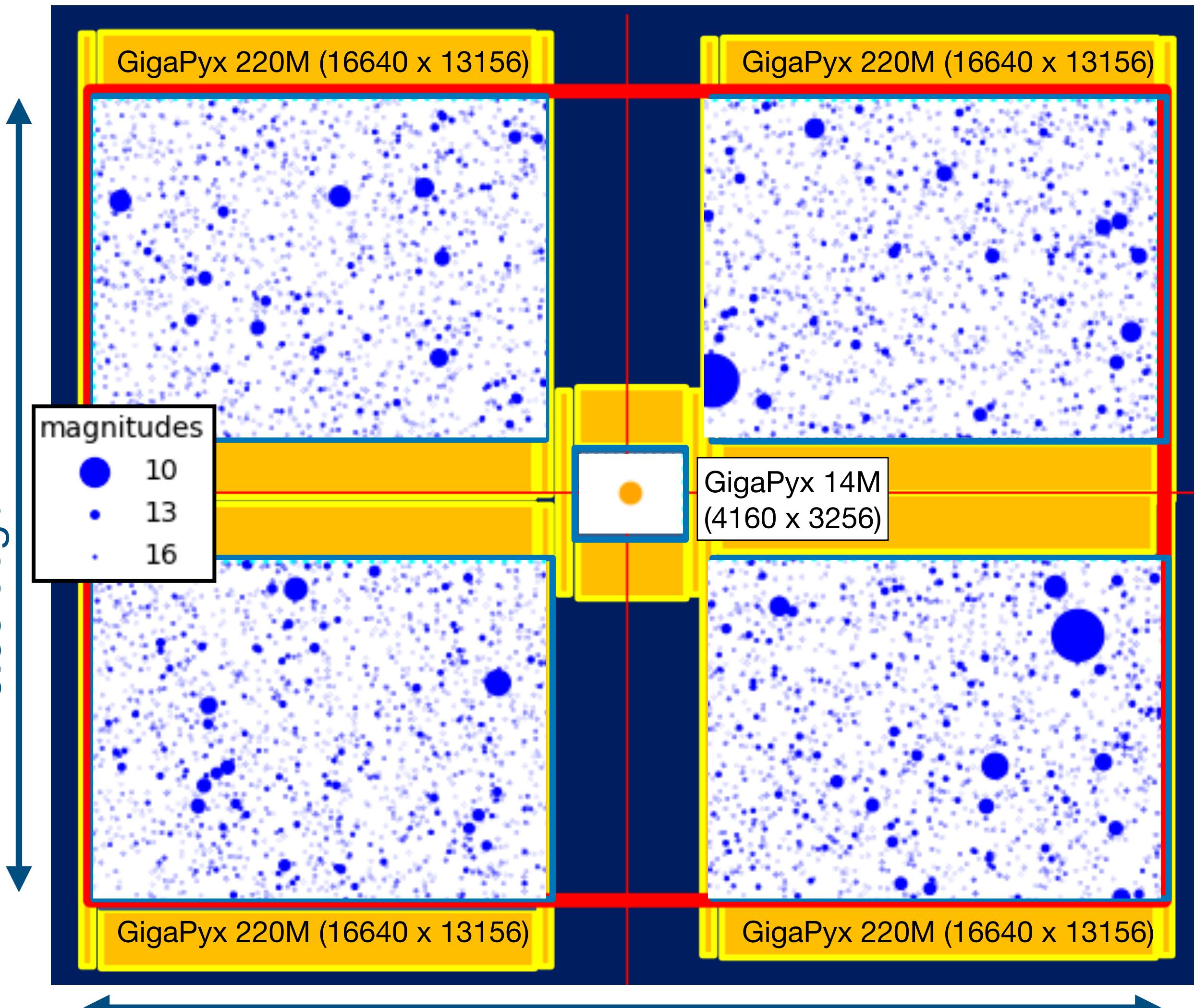
GigaPyx 46MP



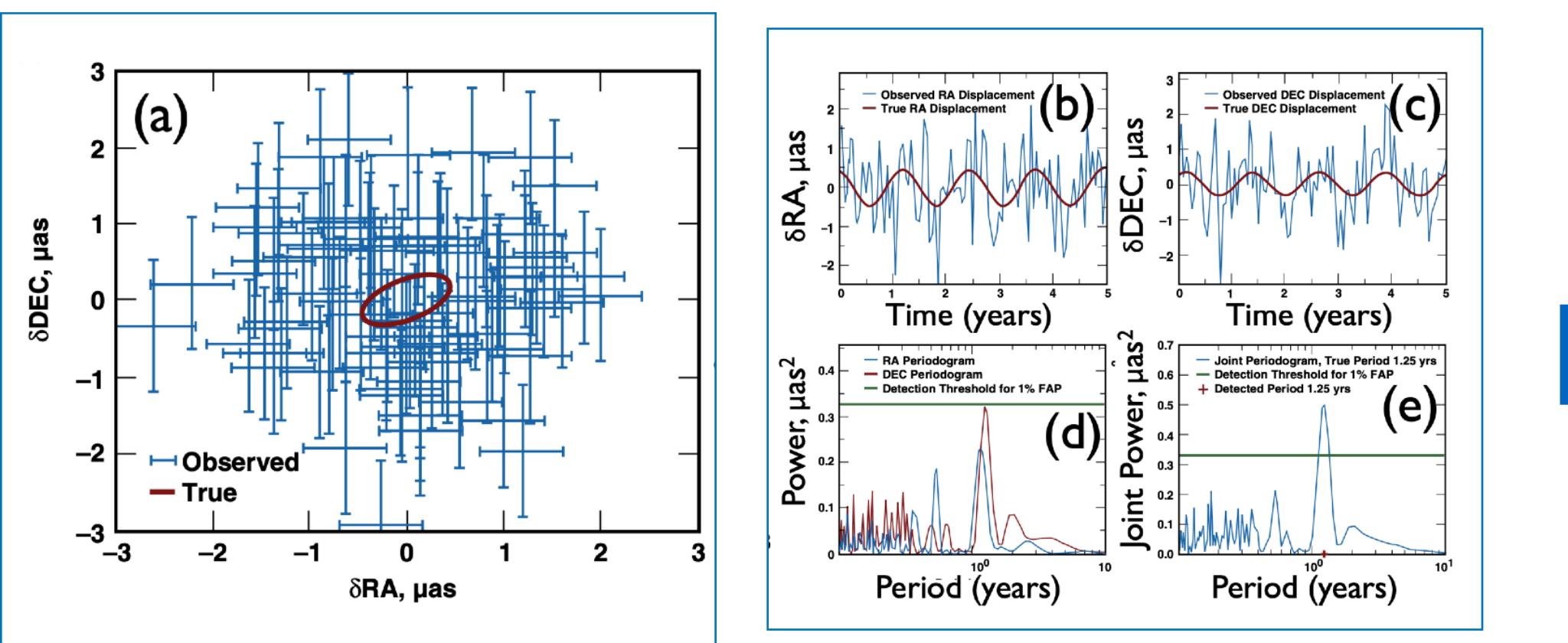
GigaPyx 220MP



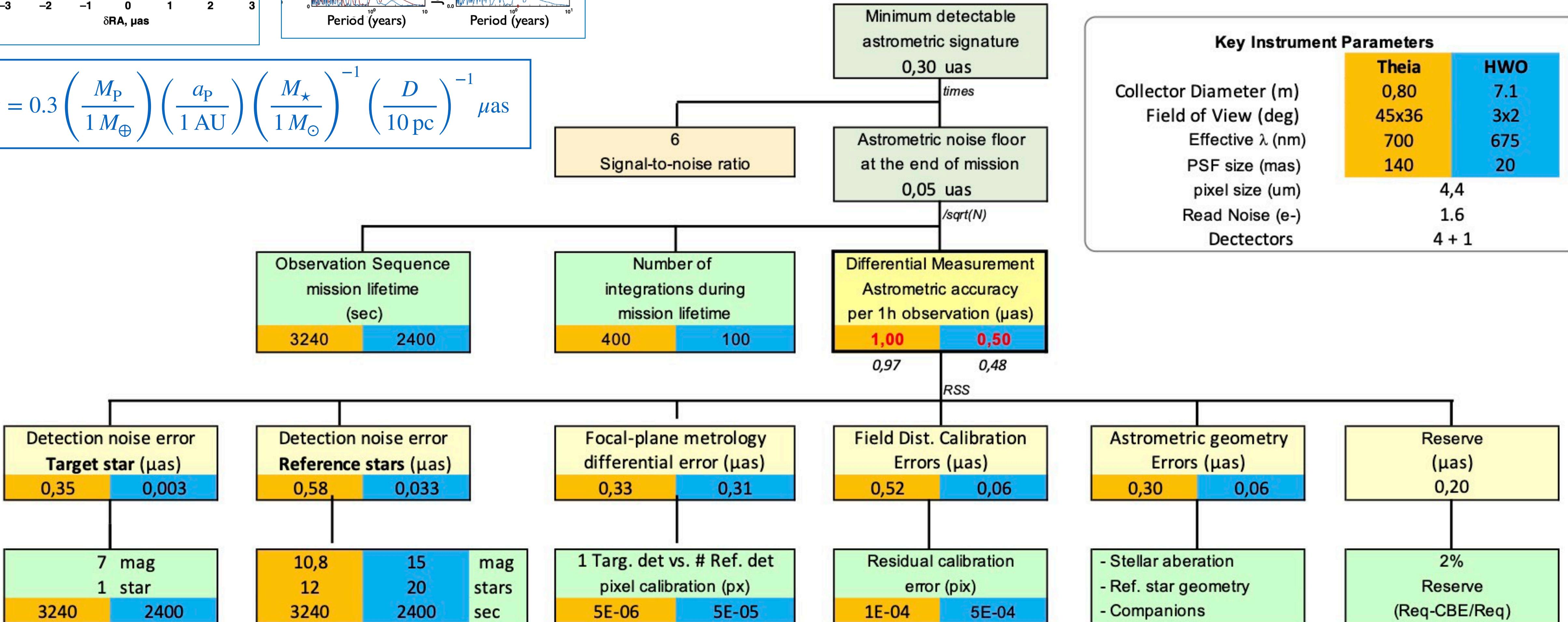
Field around ι Per (V = 4.05 mag, d = 10.58 pc, G0V)



Astrometric error budget for bright targets with Theia and HWO

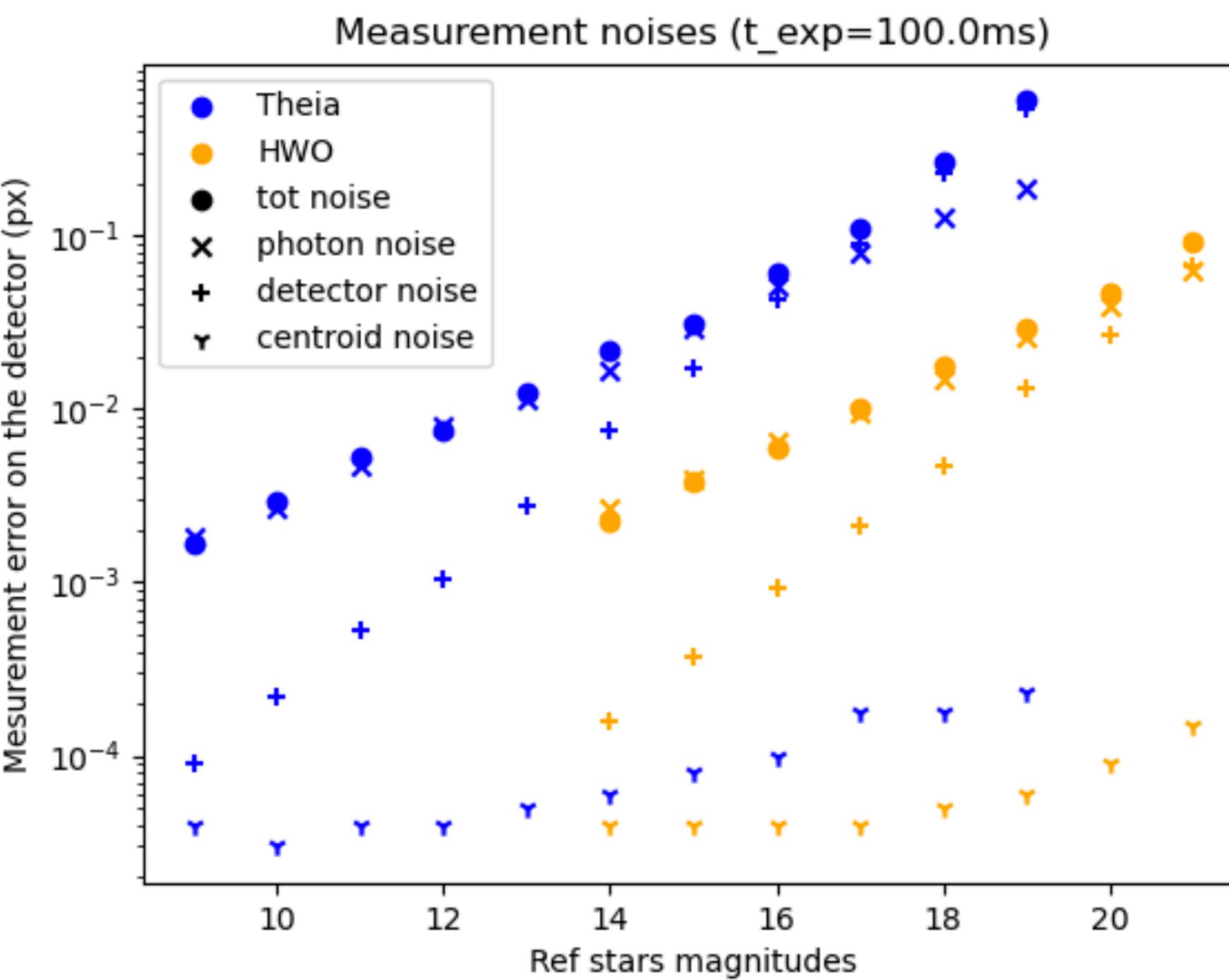


$$\alpha = 0.3 \left(\frac{M_p}{1 M_\oplus} \right) \left(\frac{a_p}{1 \text{ AU}} \right) \left(\frac{M_\star}{1 M_\odot} \right)^{-1} \left(\frac{D}{10 \text{ pc}} \right)^{-1} \mu\text{as}$$

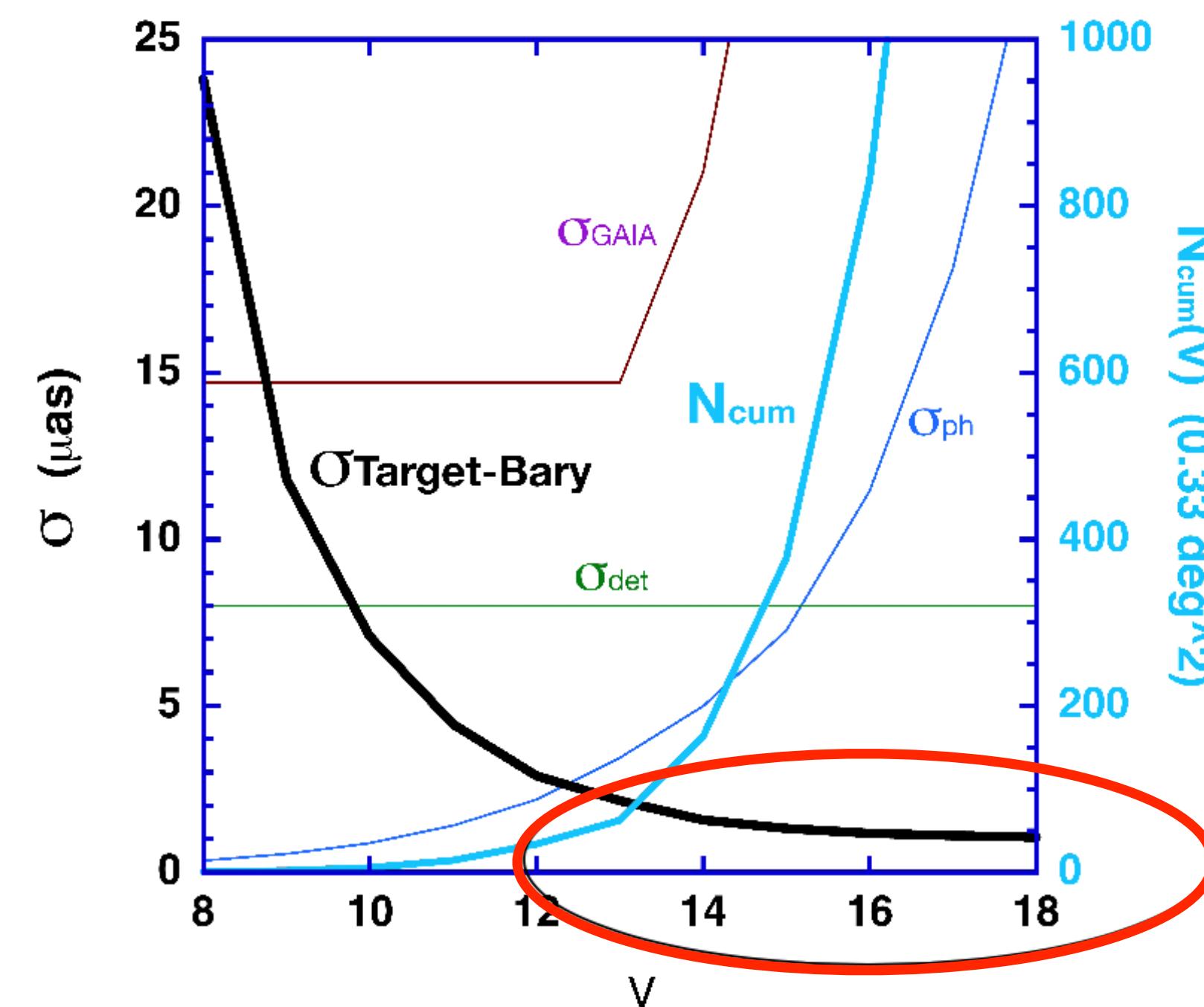


The accuracy of target position increases with number of reference stars

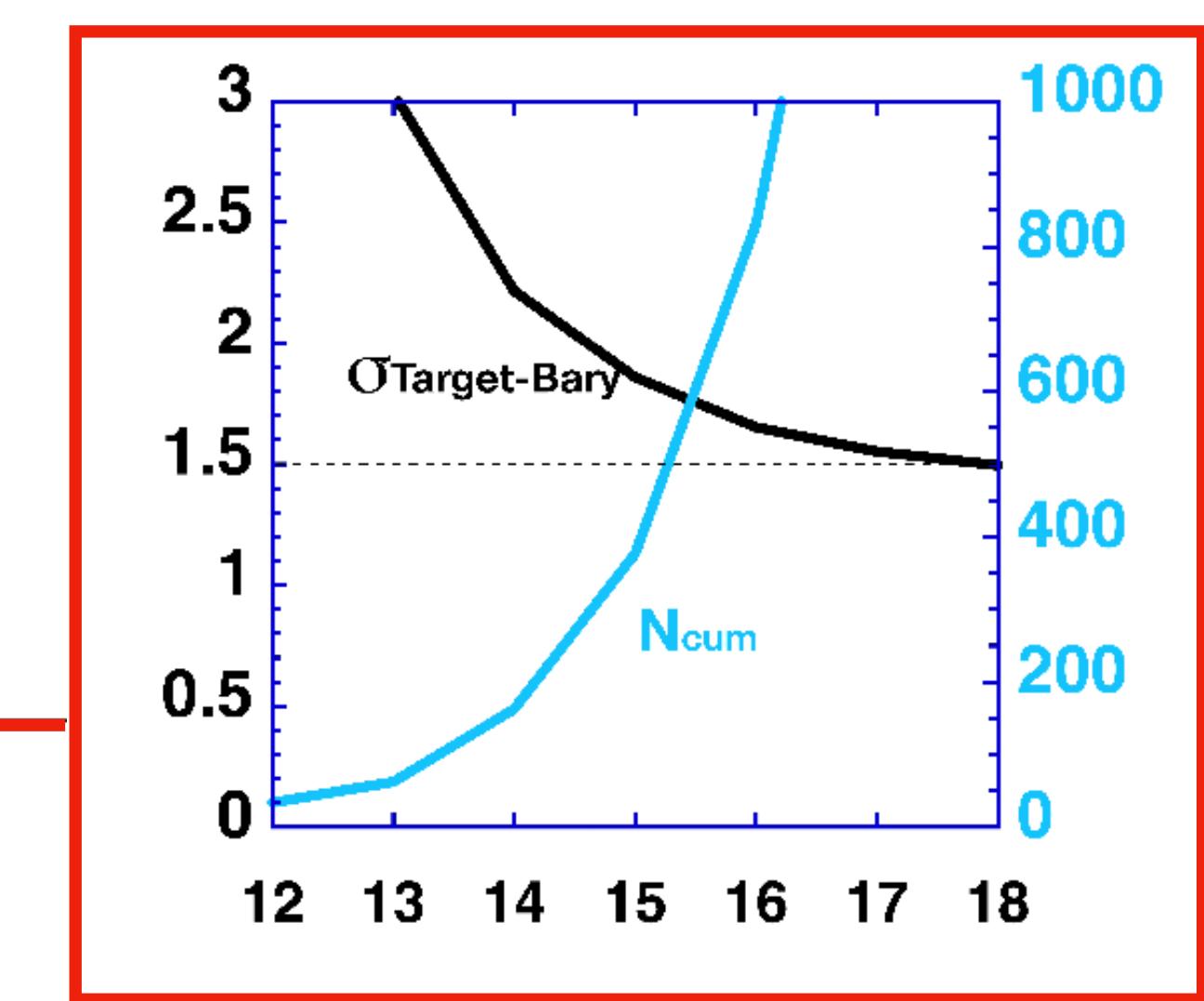
Uncertainties on reference position increases with flux, mostly limited by photon noise at the bright end and detector noise at the faint end.



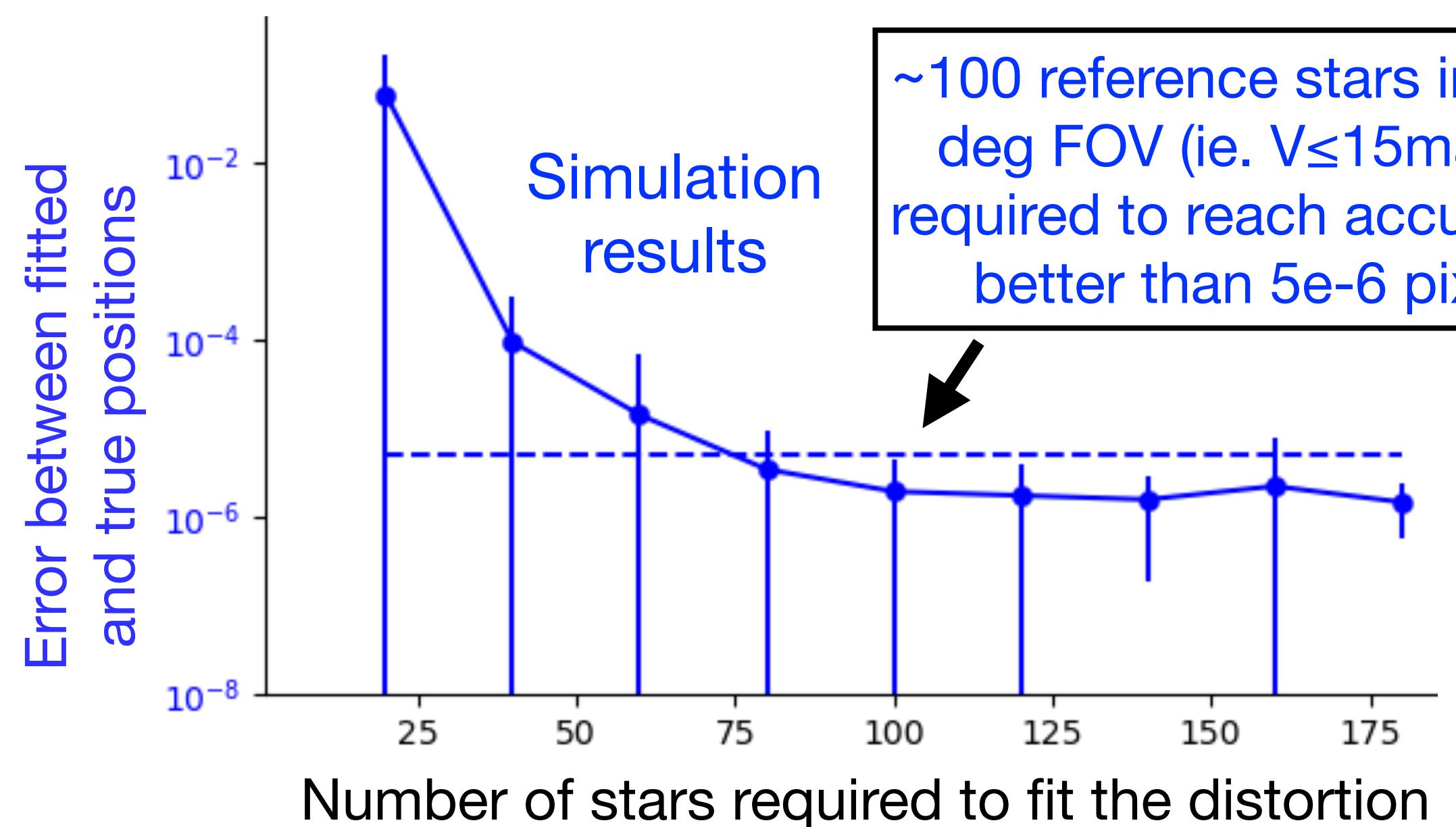
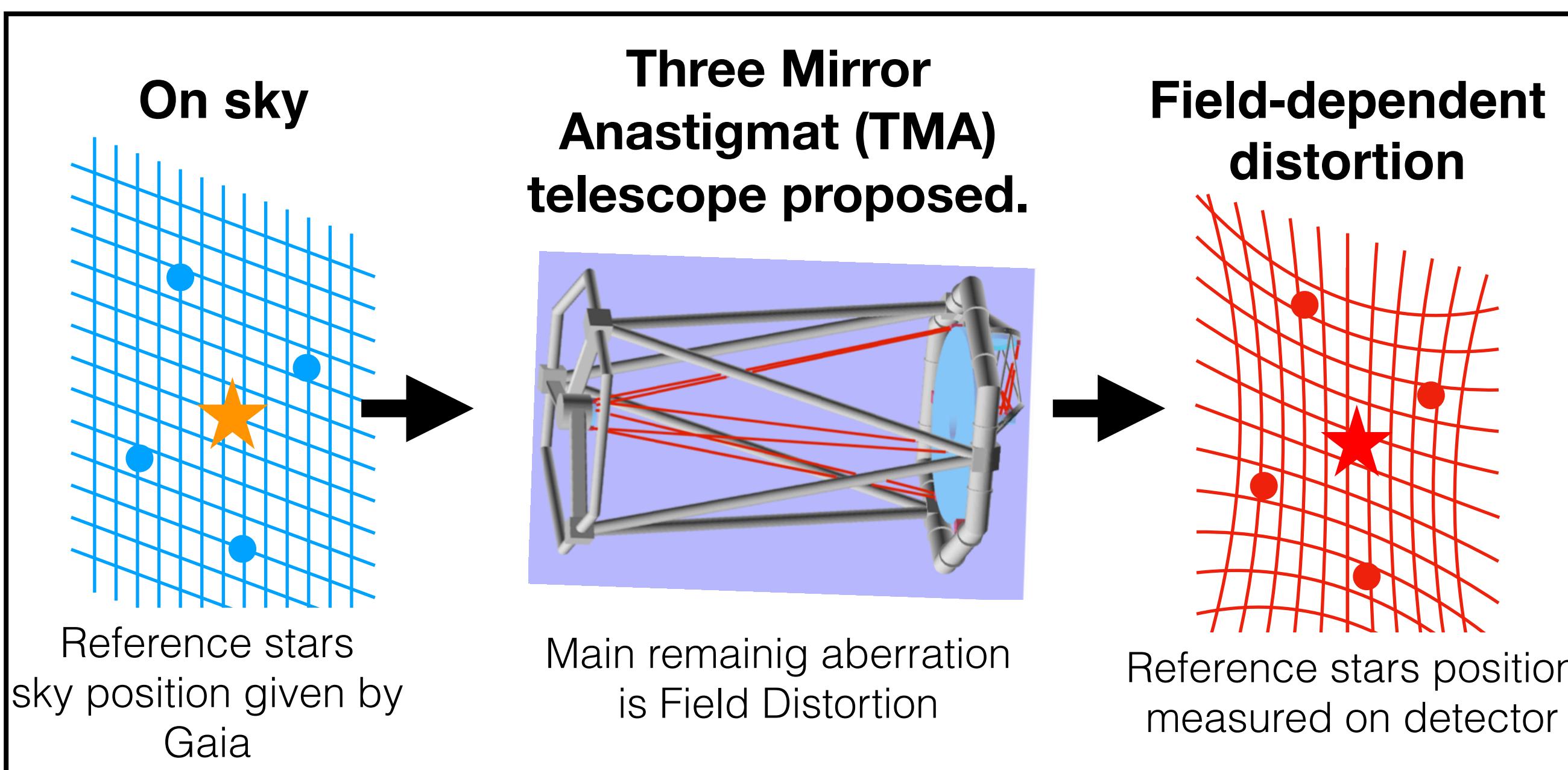
Accuracy of Gaia position for after 20 years is not sufficient, but this can be solved by using multiple reference stars and decrease with the number of references.



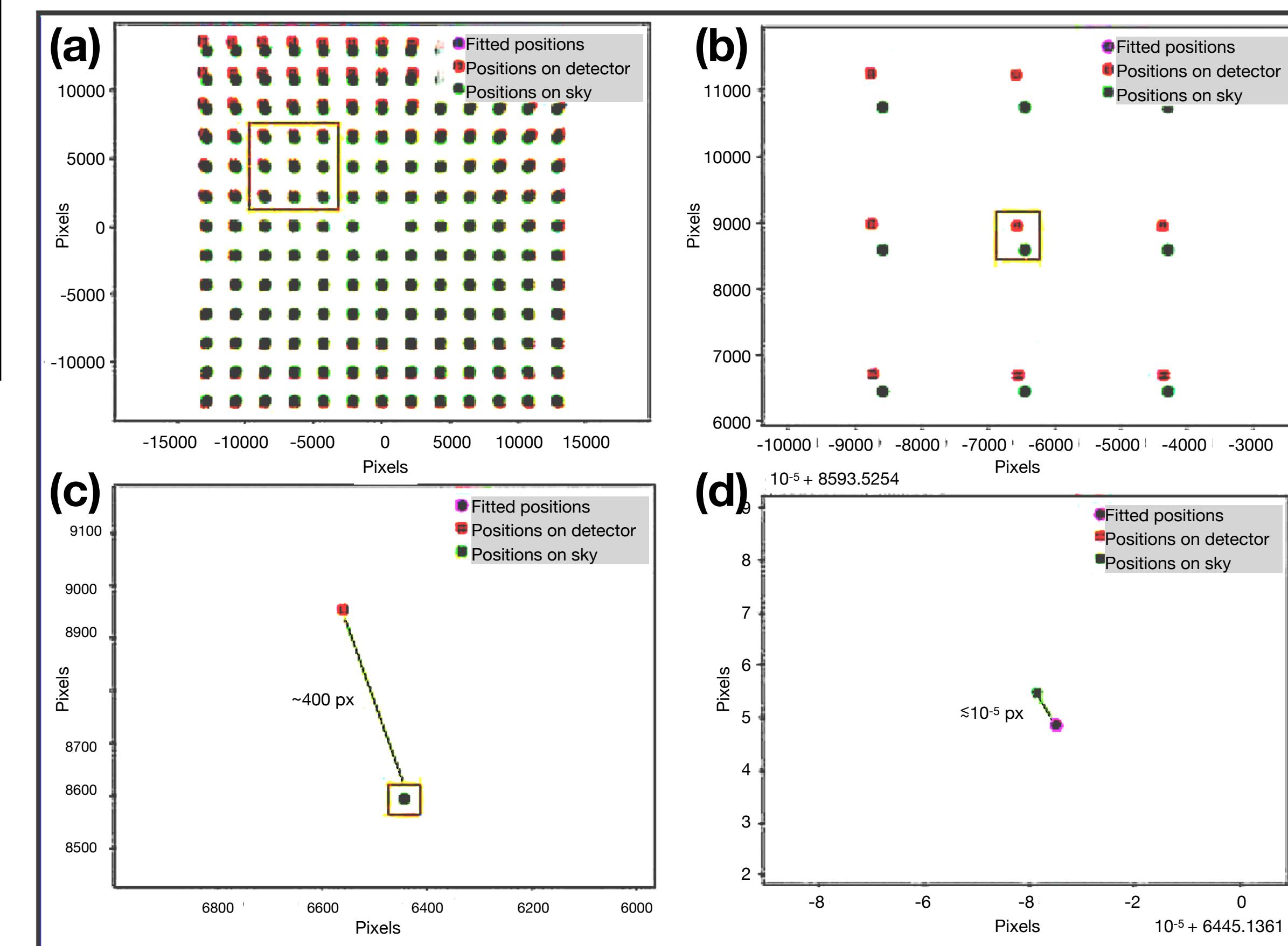
But number of reference stars increases exponentially. The final accuracy of the reference frame using Gaia data depends on each direction. However, the final precision will depend on the current mission accuracy.



Telescope calibration : using reference stars to monitor the distortion



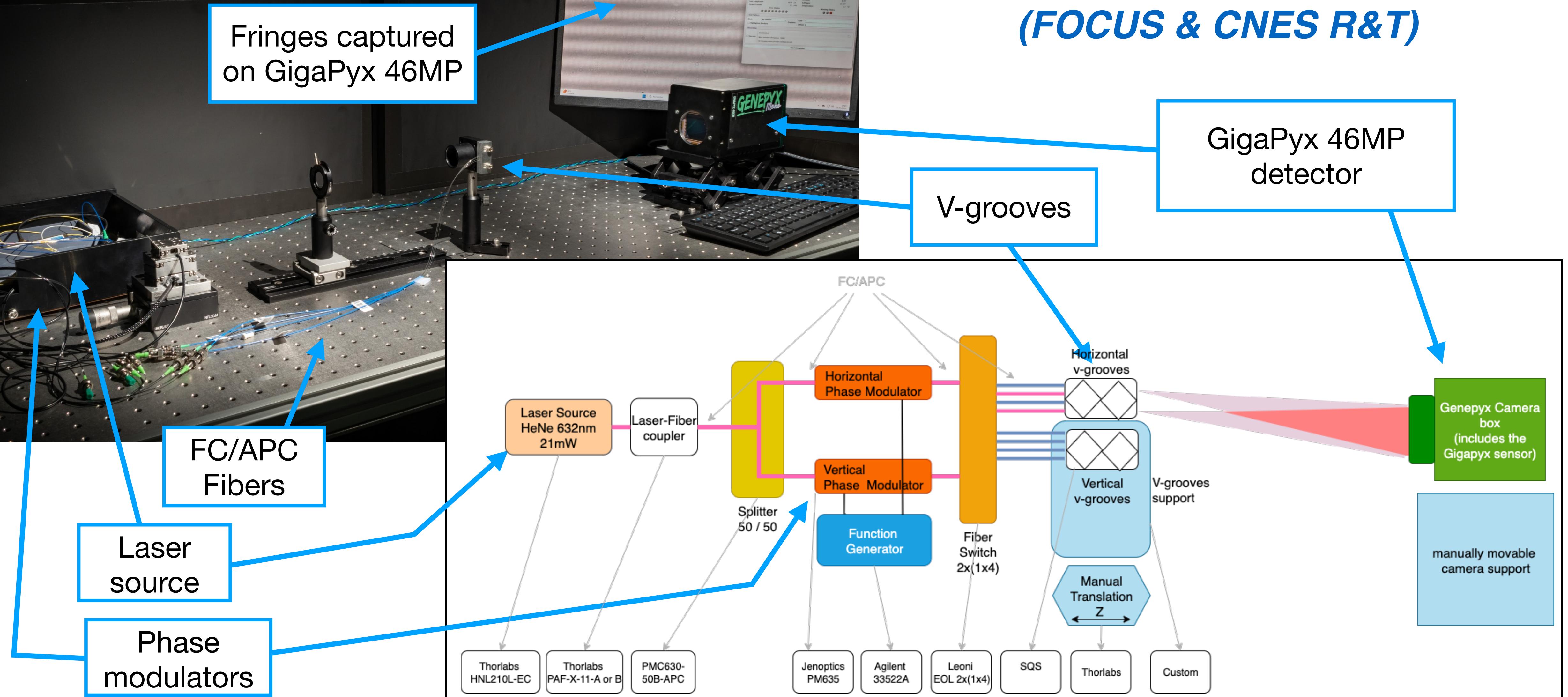
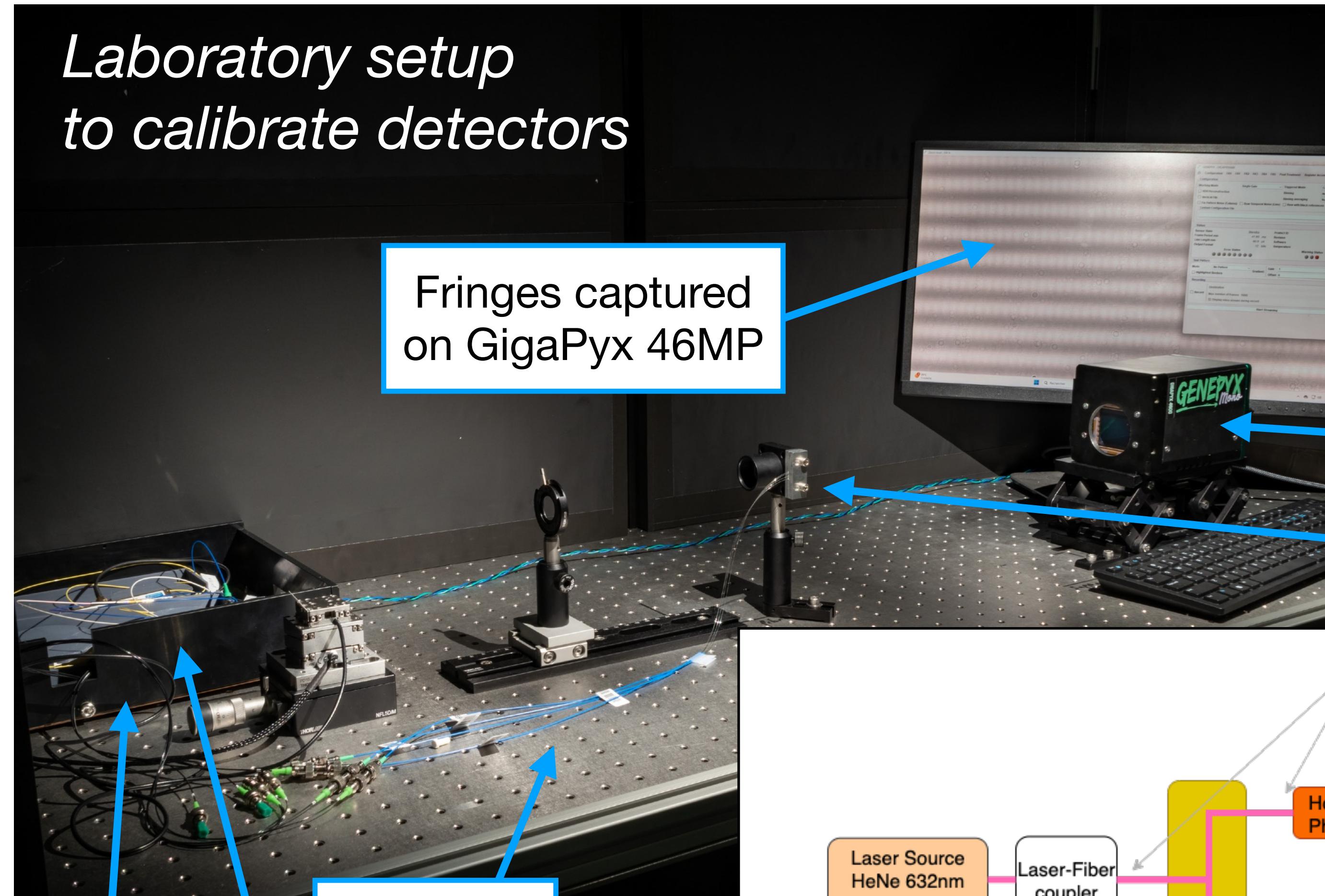
Distortion can be corrected by fitting the transformation (Sky \rightarrow Detector) as calculated by Ray-tracing (Zemax) by a 2D polynomial



Simulated field-dependent distortion and fitted position

Laboratory setup to calibrate detectors

Current lab tests at IPAG (FOCUS & CNES R&T)



Detector radiometric performance measurements

GIGAPYX 4600

46 Megapixel, BSI Rolling Shutter
High Speed HDR CMOS image sensor



Key Performances

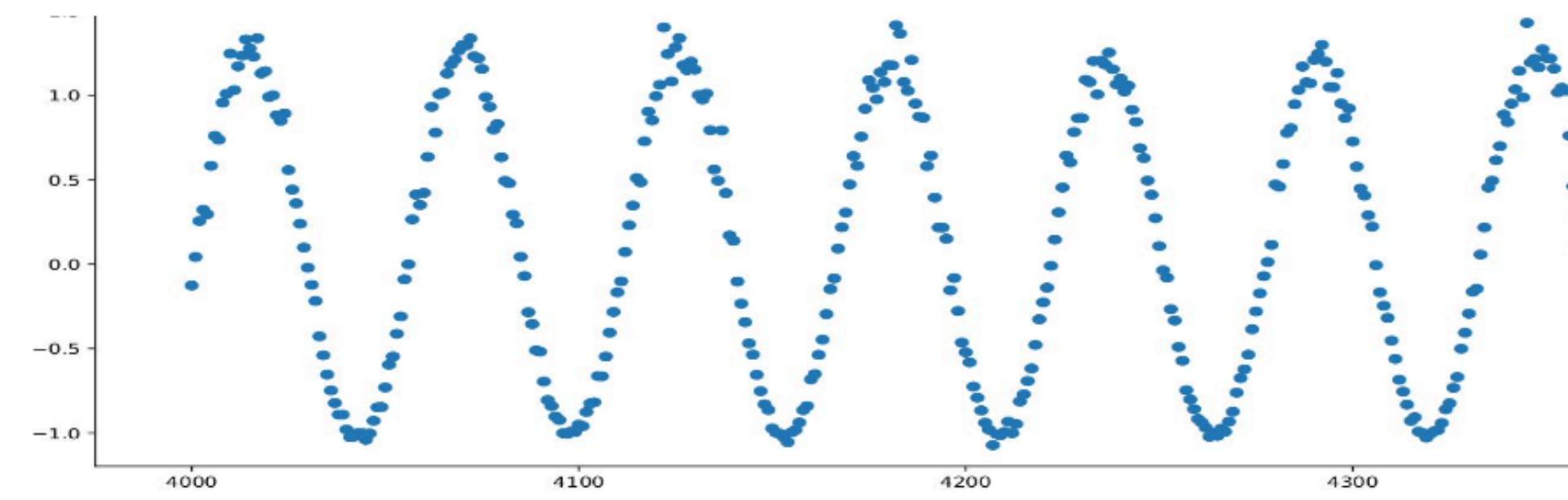
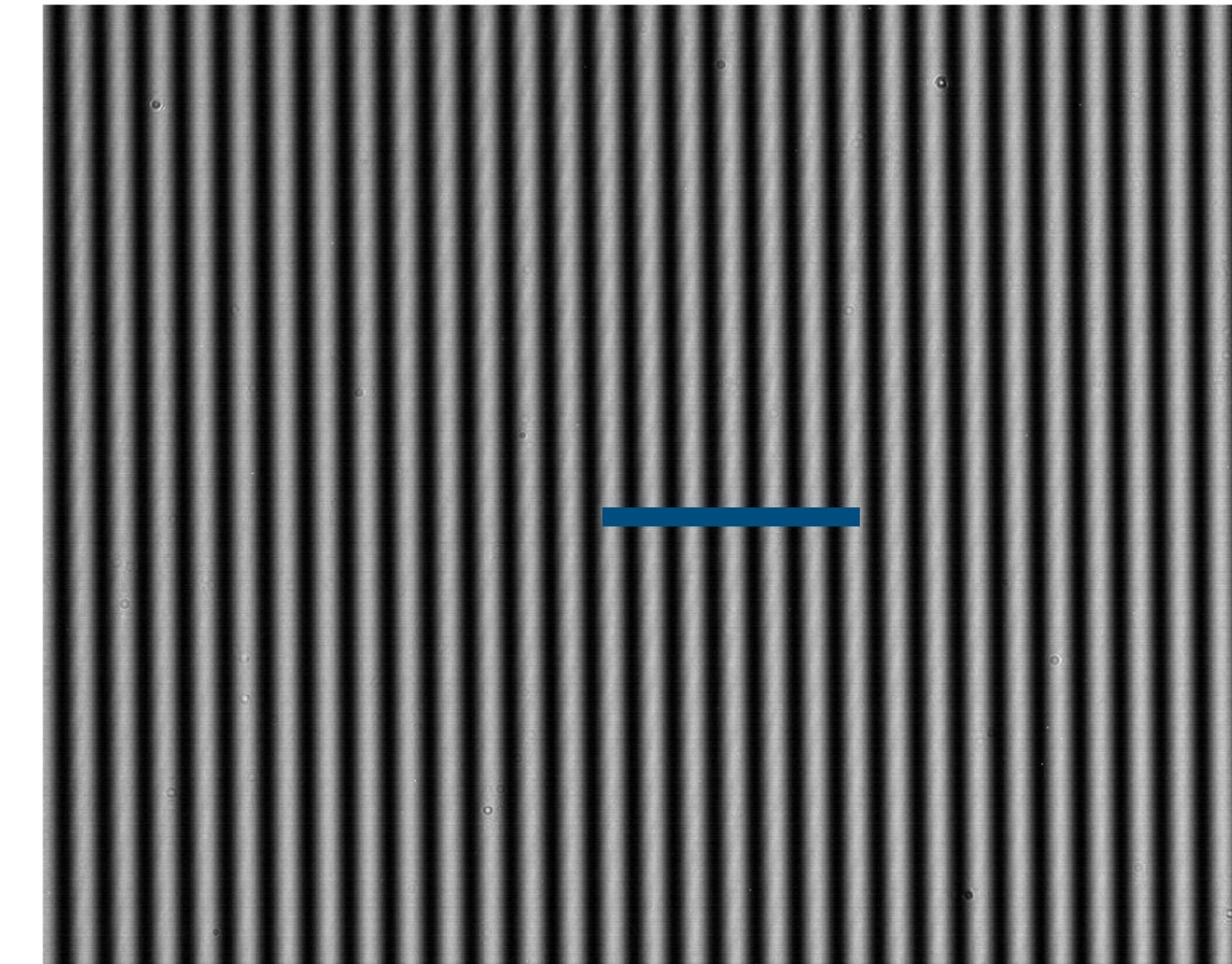
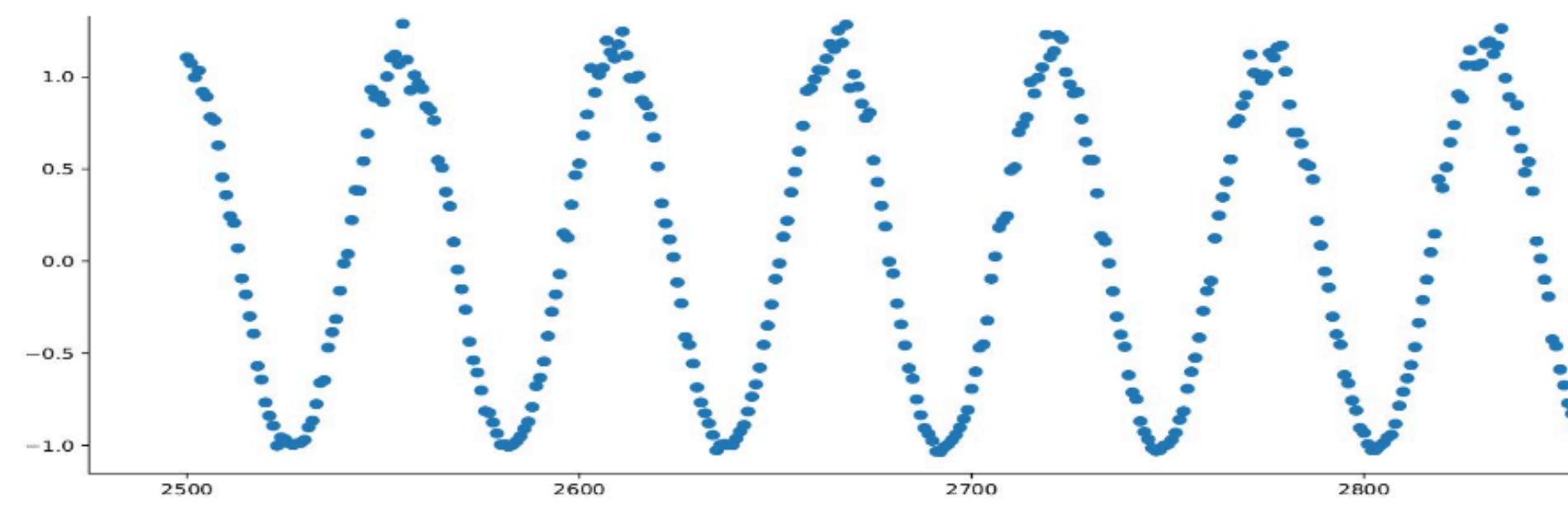
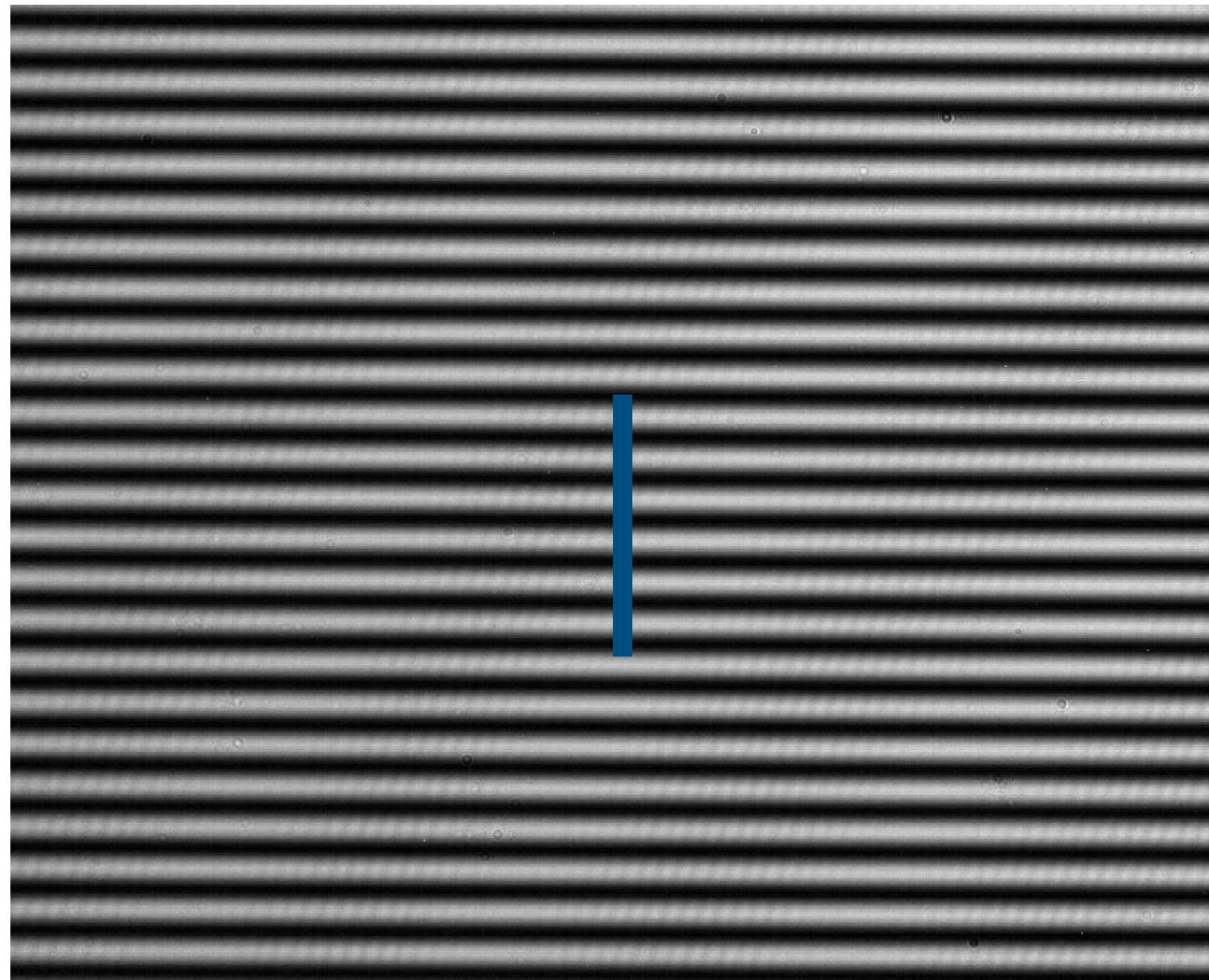
Parameter	Typical Value
Saturation Charge (linear), HG/LG	5 ke- / 50 ke-
Temporal Noise in darkness (HG) ⁽¹⁾	1.5 e- rms
Linearity Error, 5-95% QSAT _{LIN}	< 3%
Dynamic Range, HG ⁽¹⁾	70 dB
Dynamic Range, HDR ⁽¹⁾	90 dB
SNR at blending point in HDR	37 dB
Peak QE x FF, at 445 nm (mono)	80 %
Relative Illumination, up to $\pm 25^\circ$	> 90%
Dark-Current ⁽¹⁾	24 e-/s rms (@35°C)
Fixed-Pattern Noise ⁽²⁾	14 DN
Photo-Response Non-Uniformity ⁽²⁾	< 2%
Frame-rate, FF, 12 bits, HG/LG	152 FPS
Frame-rate, 8K, 12 bits, HG/LG	192 FPS
Frame-rate, FF, 13 bits, HDR	54 FPS
Frame-rate, 8K, 13 bits, HDR	63 FPS
Power-consumption, standby	< 150 mW
Power-consumption, full operation ⁽³⁾	< 4.1W

Our measurements

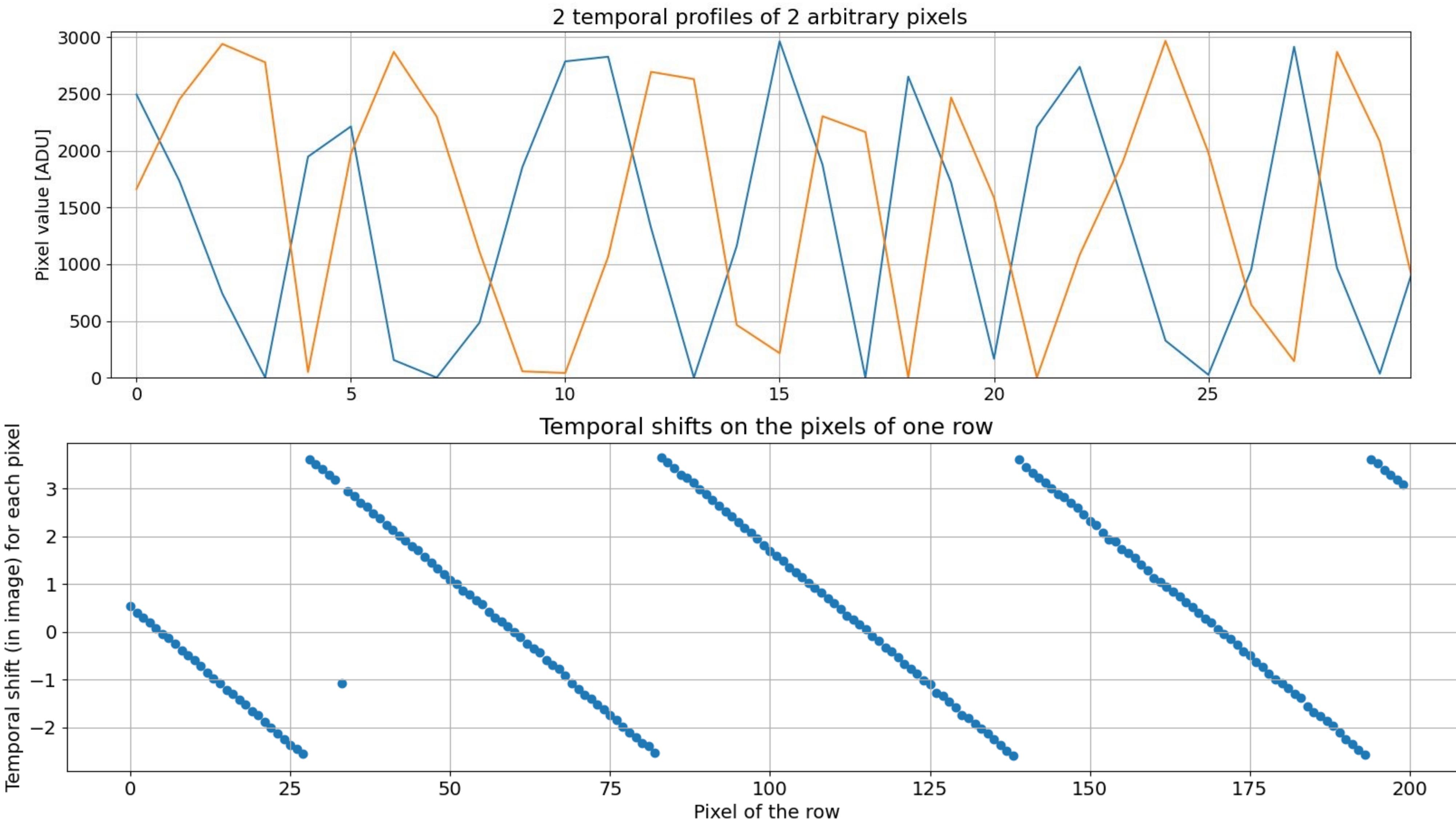
```
median_bias_(ADU): 377.0
std_bias_(ADU): 60.9961
median_dark_current_(ADU/ms): 0.0387
std_dark_current_interpx_(ADU/ms): 0.011
std_dark_current_1px_(ADU/ms): 0.0002
linearity_error_(%): 0.5154
median_roq_noise_(ADU): 0.7798
std_roq_noise_(ADU): 0.2203
median_gain_(ADU/e-): 0.7105
std_gain_(ADU/e-): 0.0359
PRNU_tot_(%): 2.2207
PRNU_center_(%): 1.7011
PRNU_HF_(%): 2.7931
```

	PYXALIS	IPAG measurements	
	(e-)	(ADU)	(e-)
Conversion factor (ADU/e-)	0.7	-	0.71
Read-out noise	1.6		
Dark current (/ms)	24	39	27
PNRU	<2%		2.2%

First fring measurements on a 46MP detector



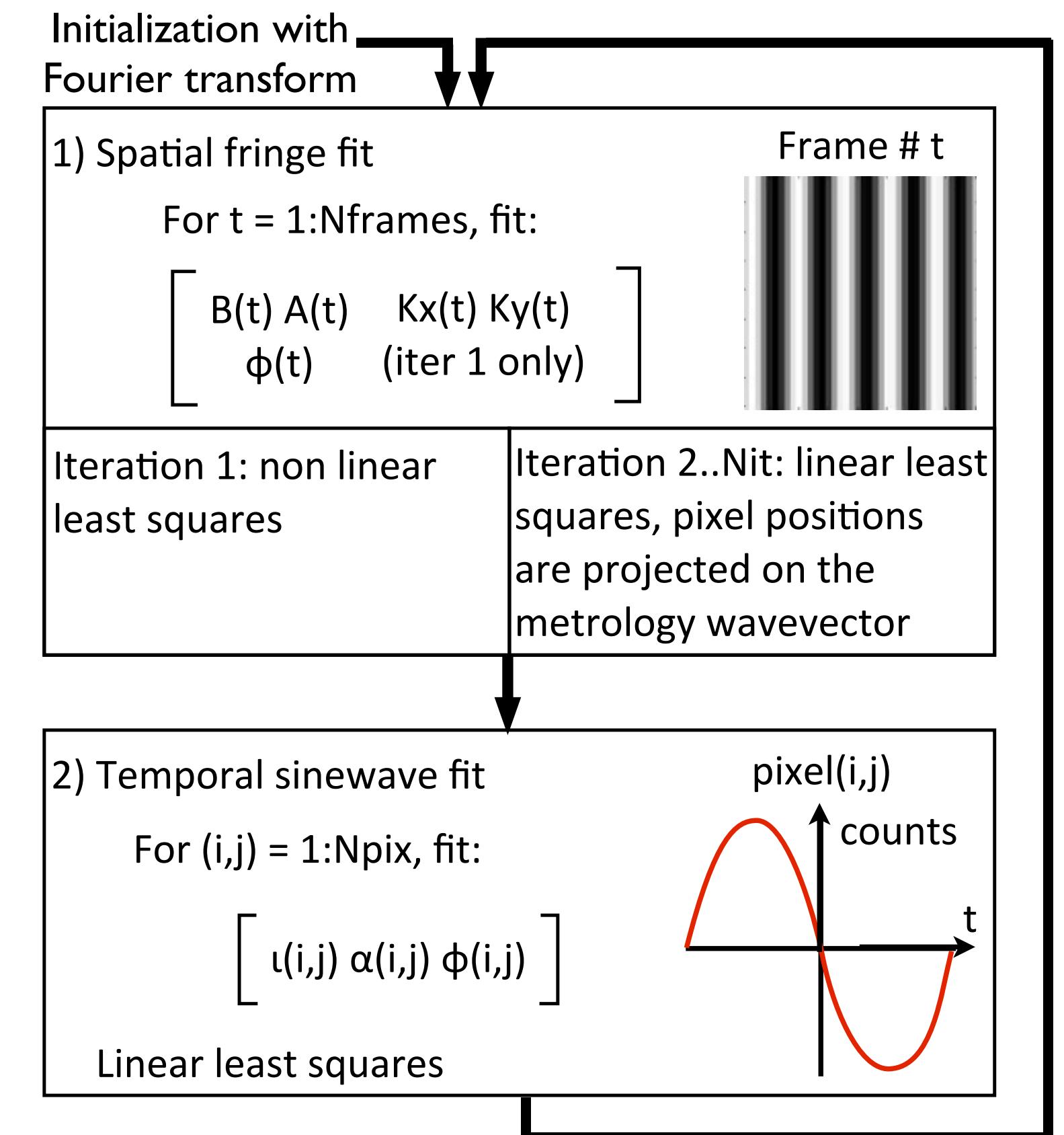
Temporal correlation of the interferometric signal



Retrieving pixel positions at sub-millipixel accuracy

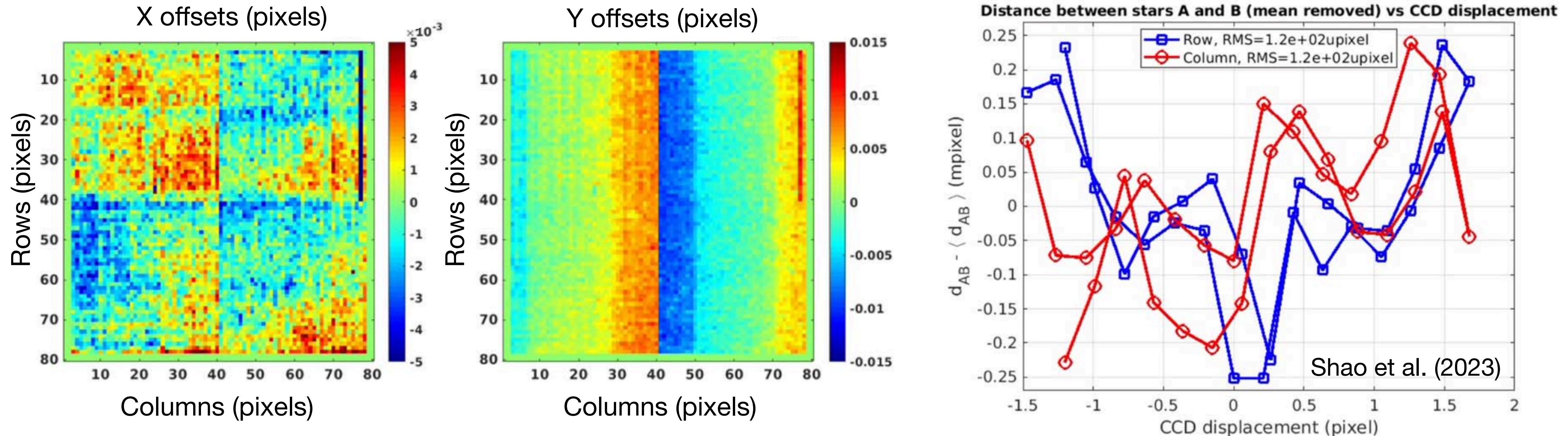
$$I_{ij}(t) = B(t) \ i_{ij} + A(t) \ \alpha_{ij} \ \sin \left[i K_x(t) + j K_y(t) + \phi(t) + \delta_{x,ij} K_x(t) + \delta_{y,ij} K_y(t) \right]$$

Notation	Name	Absorbed noises
$B(t)$	Average intensity	Laser flux, offset fluctuations
i_{ij}	Intensity carrier	Photo response non uniformity (PNRU)
$A(t)$	Average fringe amplitude	Laser flux, polarisation fluctuations
α_{ij}	Fringe relative amplitude	Photo response non uniformity (PNRU)
$K_x(t), K_y(t)$	Metrology wavevector	Laser freq. fluctuation, thermal expansion
$\phi(t)$	Differential phase	Phase jitter (thermal and mechanical)
$\delta_{x,ij}, \delta_{y,ij}$	Pixel offsets (x and y directions)	-



Crouzier et al. (2016)

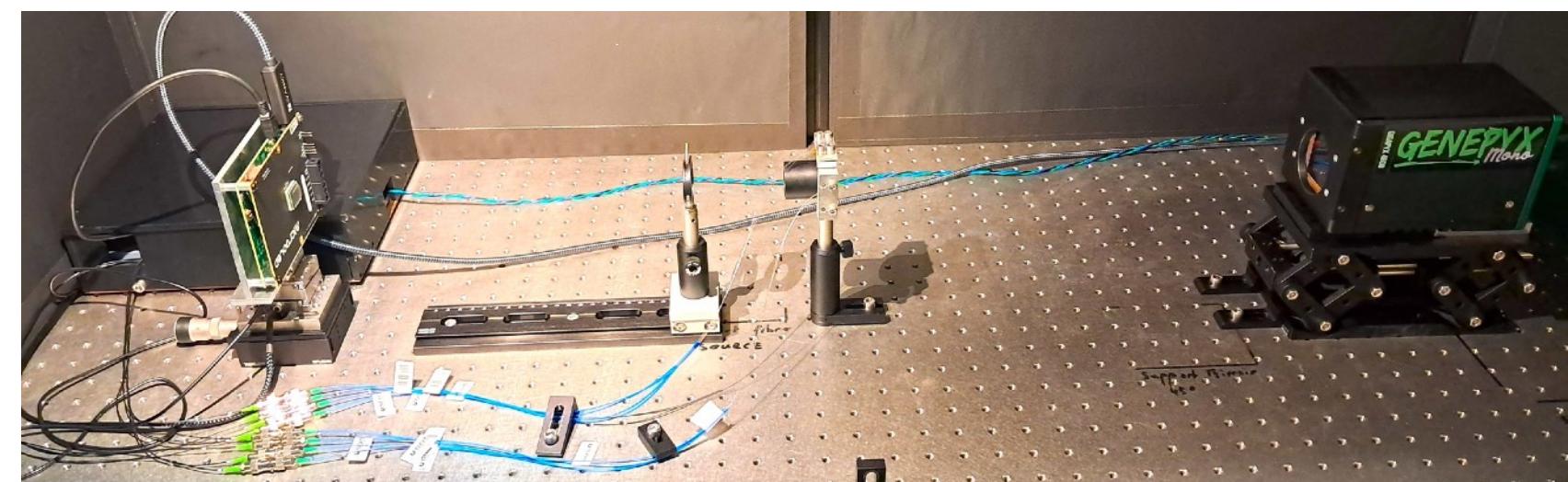
Detector interferometric measurements



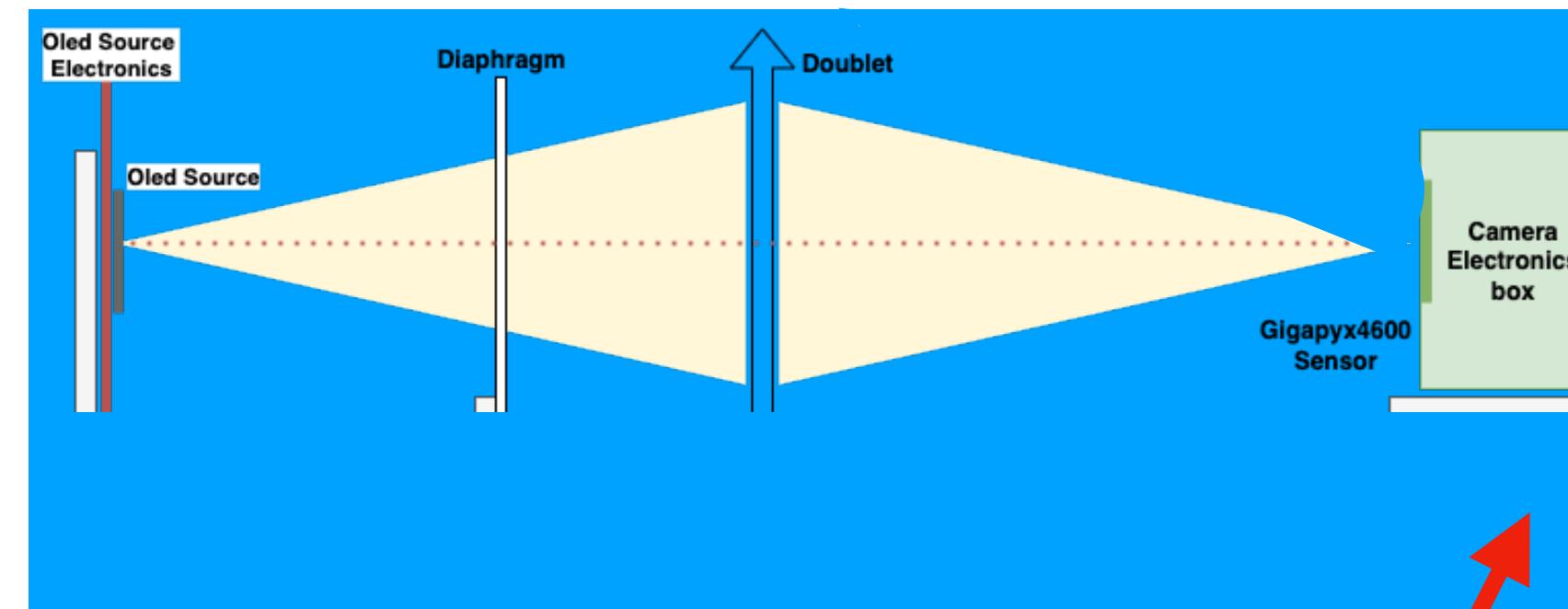
Best results so far:

- IPAG/CNES: 6×10^{-5} pixels (Crouzier et al. 2016, A&A 595, A108)
- JPL/VESTA: 3×10^{-5} pixels (Shao et al. 2023, PASP 135, 074502)

Optical calibration in the lab



On the OLED
micro-display



On the GigaPyx
46MP detector

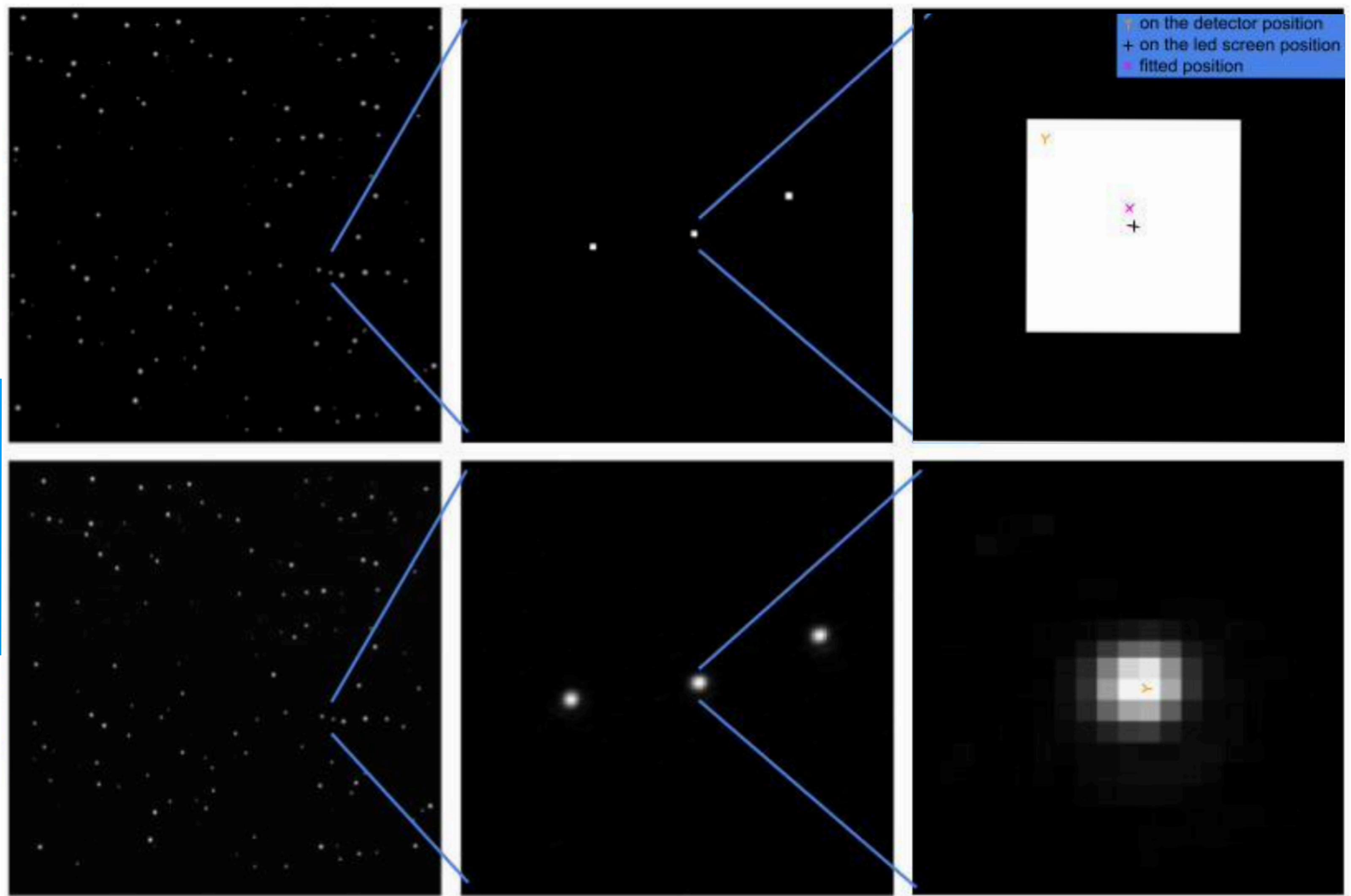
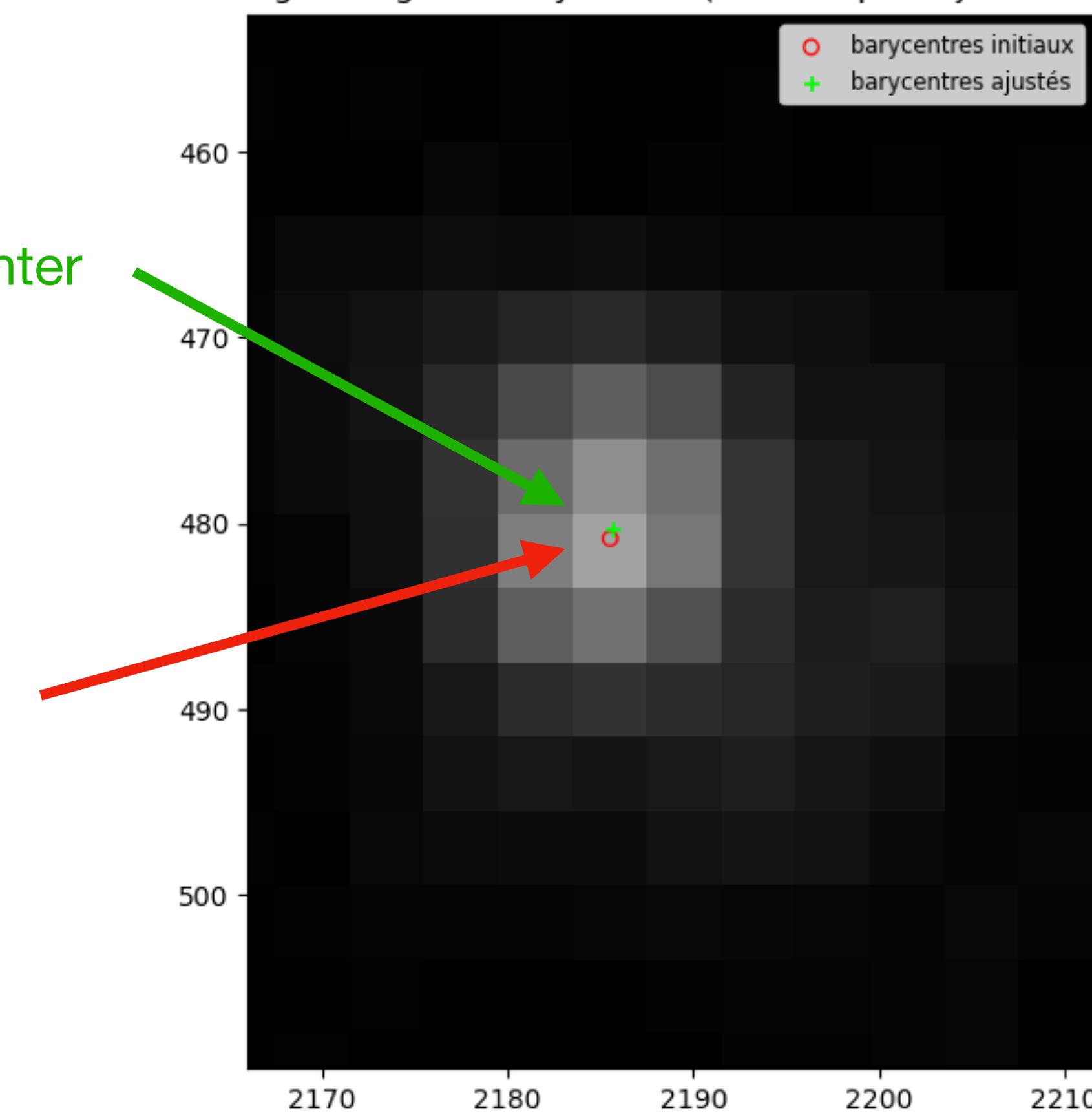


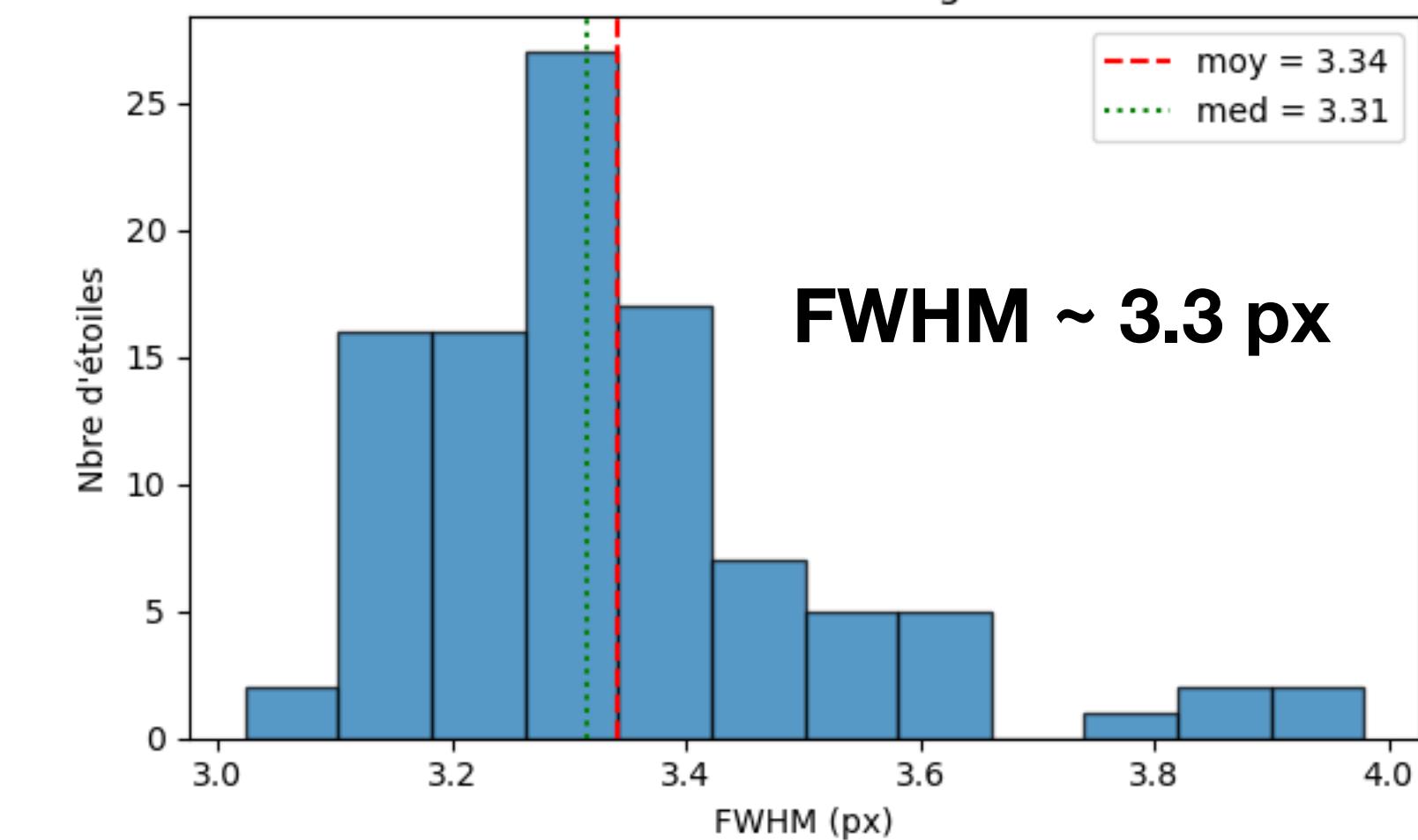
Image data processing

Gaussian fit barycenter

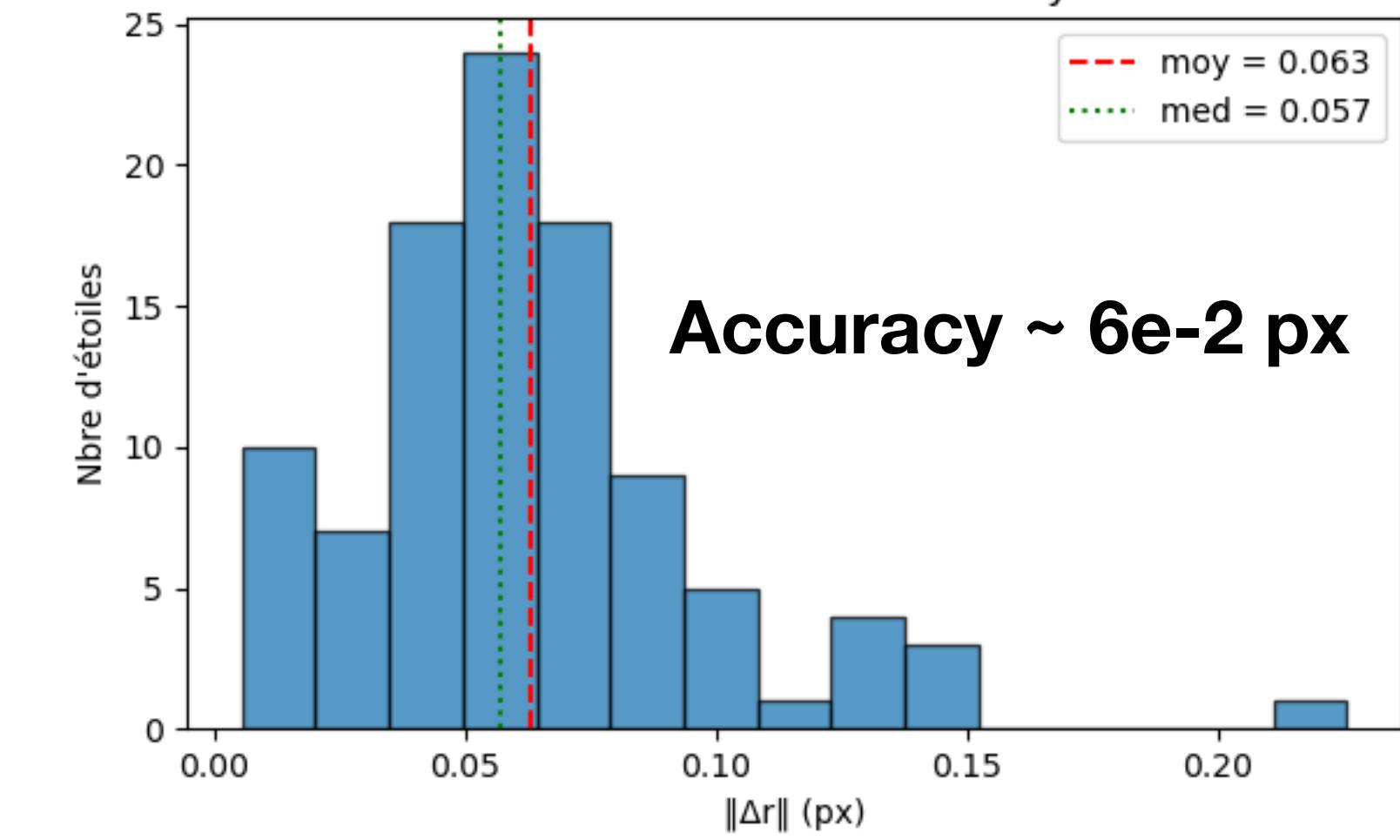
Image d'origine - barycentres (avant / après ajustement)



Distribution des FWHM gaussiens



Distribution des corrections de barycentres



Quite promising ! We need to make sure that we are meeting the flux requirement.

Conclusion and perspectives

- We have shown that the CMOS 46MP Gigapyx should be a viable technology for high precision astrometry
- The lab measurements are reaching the company announced performance
- The test bench in the lab is operationnal
- We are measuring fringes and temporal modulation, but we are not yet at the pixel position calibration
- The lab simulation of optical distortion correction is working at 1e-2 level, but not yet reaching 1e-4 pixel;
- For GaiaNIR, the detector technology is different but the process is the same with other materials.